

ERROR RECOGNITION & IMAGE ANALYSIS



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Based on the lecture given by Gustaff van Moorsel at
NRAO's 2010 Synthesis Imaging Workshop

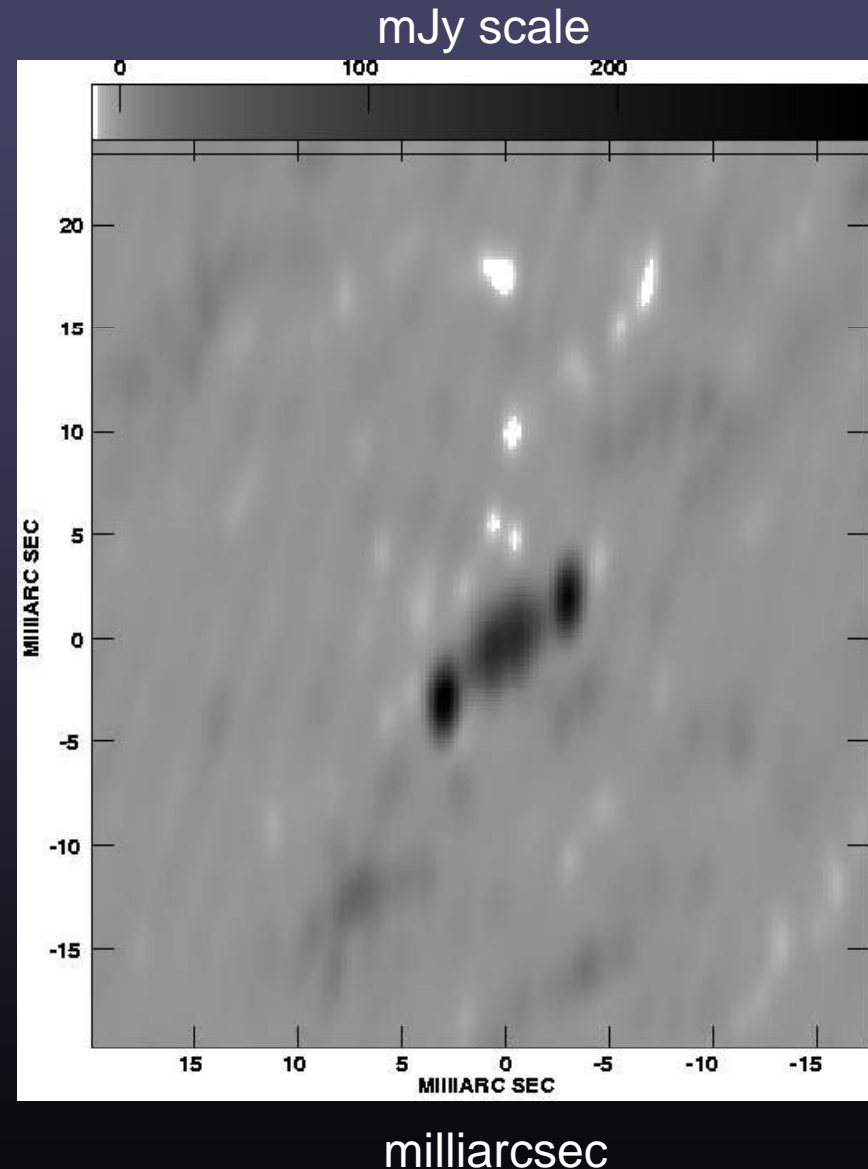
INTRODUCTION

- Why are these two topics – ‘Error Recognition’ and ‘Image Analysis’ in the same lecture?
 - **Error recognition** is used to determine defects in the (visibility) data and image during and after the ‘best’ calibration, editing, etc.
 - **Image analysis** describes the almost infinite ways in which useful insight, information and parameters can be extracted from the image.
- Perhaps the two topics are related to the reaction one has when looking at an image after ‘good’ calibration, editing, self-calibration, etc.
- **If the reaction is:**

OBVIOUS IMAGE PROBLEMS

Yuck!!

- This can't be right. This is either the most remarkable radio source ever, or I have made an error in making the image.
- Clear signs of problems:
 - Image rms > expected rms
 - Unnatural features in the image
- How can the problems be found and corrected?



HIGH QUALITY IMAGE

Great!!

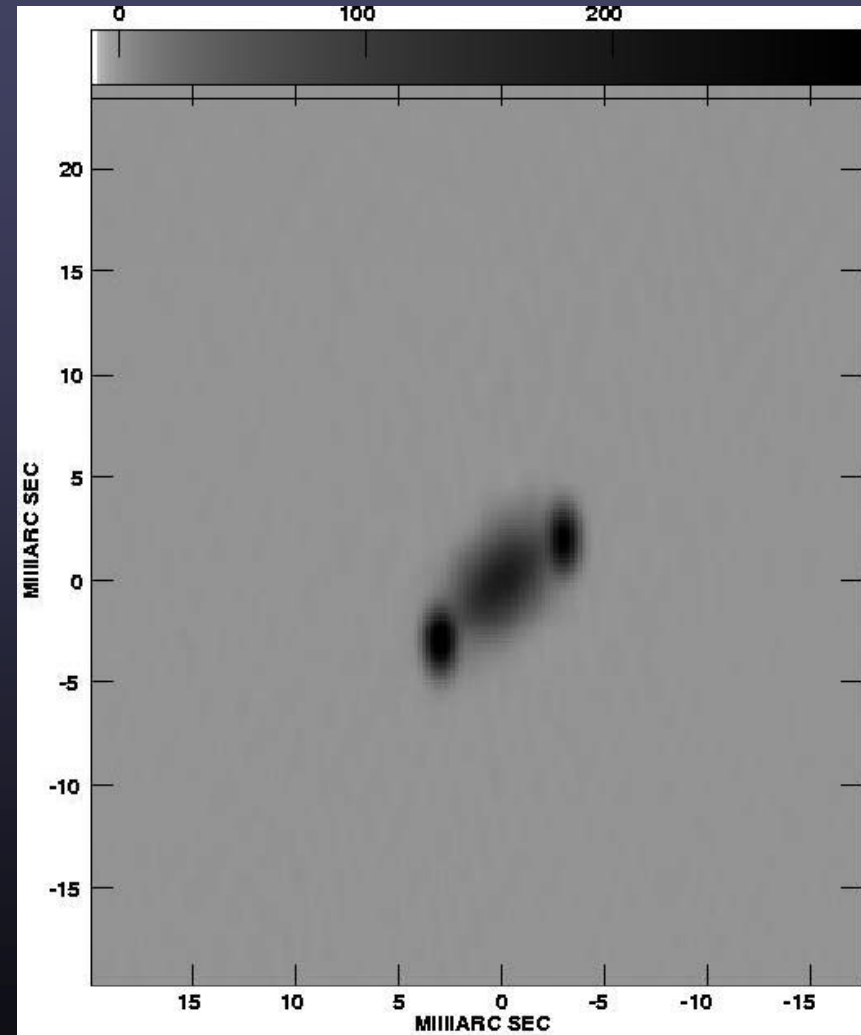
After lots of work, I can finally analyze this image and get some interesting scientific results.

What were defects?

1. Two antennas had 10% calibration errors
2. one with a 5 deg error
3. A few outlier data points.

This part of the lecture

How to find the errors and remove them.



milliarcsec

GENERAL PROCEDURE

We assume that the data have been edited and calibrated reasonably successfully (earlier lectures). Self-calibration is sometimes necessary.

So, the first serious display of an image leads one—

- to inspect again and clean-up the data repeating some or all of the previous reduction steps.
 - removal of one type of problem can reveal next problem!
- once all is well, proceed to image-analysis and obtaining scientific results from the image.

But, a digression on data and image display.

First: Images

IMAGE DISPLAYS (1)

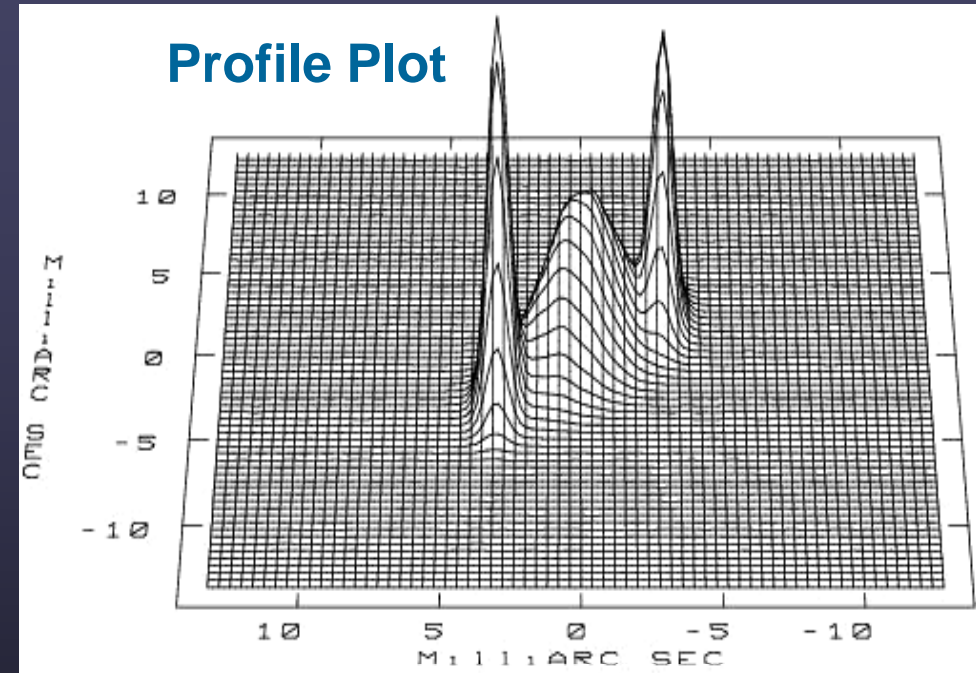
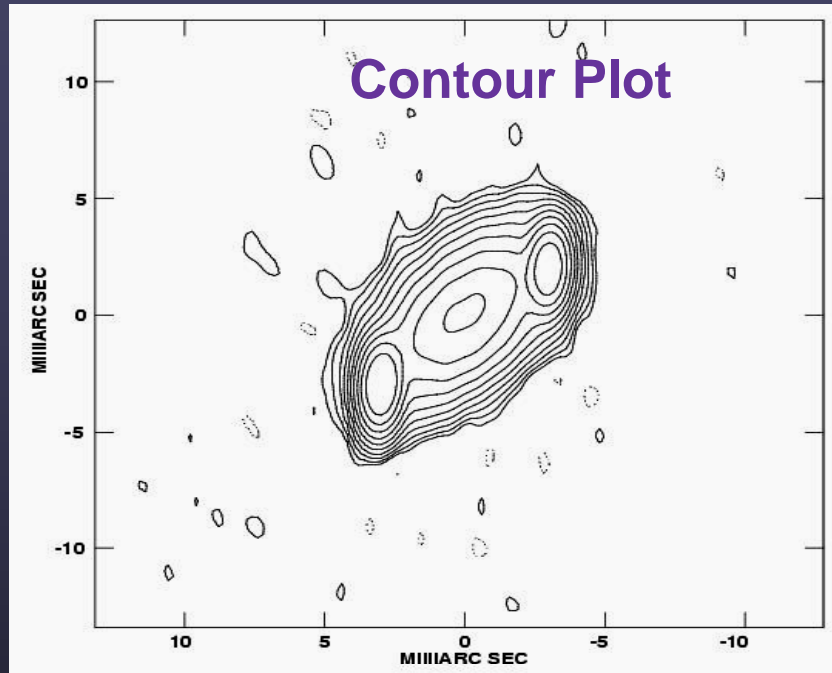
	Pixel values																											
	235							245							255							265						
287	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
285	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
283	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	0	0	0	0
281	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	2	3	3	3	4	3	1	0	0	0	0
279	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	2	3	4	4	5	5	8	12	8	3	1	0	0
277	0	0	0	0	0	0	0	0	0	0	0	0	0	1	2	3	5	7	7	8	9	9	19	32	22	6	1	0
275	0	0	0	0	0	0	0	0	0	0	0	0	0	1	2	4	6	9	13	14	15	14	16	40	72	47	12	2
273	0	0	0	0	0	0	0	0	0	1	1	1	2	4	8	12	17	22	23	24	22	27	77	136	87	19	2	0
271	0	0	0	0	0	0	0	0	0	1	1	2	4	8	15	21	28	35	36	37	33	43	126	217	132	28	3	0
269	0	0	0	0	0	0	0	0	0	1	3	4	8	15	25	34	44	54	54	53	48	61	173	298	168	34	3	0
267	0	0	0	0	0	0	0	0	0	1	2	4	8	14	25	40	52	67	79	77	74	63	75	199	316	177	34	3
265	0	0	0	0	0	0	0	0	0	1	3	7	14	24	40	60	77	97	109	102	93	74	79	191	289	155	29	3
263	0	0	0	0	0	0	0	1	2	5	11	22	37	58	86	108	130	137	123	105	79	73	154	220	113	20	2	0
261	0	0	0	0	0	0	0	1	1	3	8	17	33	54	81	116	139	156	156	133	107	75	61	106	140	69	12	2
259	0	0	0	0	0	0	0	1	2	5	12	24	45	72	105	143	182	170	161	131	99	66	47	64	75	36	6	1
257	0	0	0	0	0	0	0	2	4	8	18	32	58	88	124	160	171	169	152	118	86	55	36	36	36	16	3	1
255	0	0	0	0	0	0	0	1	2	7	16	27	42	70	101	135	162	164	156	134	100	71	44	27	20	16	7	1
253	0	0	0	0	0	0	0	1	4	15	34	43	51	77	105	133	150	146	135	112	81	56	34	19	11	7	3	1
251	0	0	0	0	0	0	0	1	8	34	73	70	59	79	100	120	130	122	110	88	61	41	24	12	6	3	1	0
249	0	0	0	0	0	0	0	1	2	14	69	141	112	85	73	87	100	106	96	83	64	43	27	14	7	3	1	0
247	0	0	0	0	0	0	0	1	3	23	121	238	167	69	62	69	77	81	70	58	42	26	16	8	3	1	0	0
245	0	0	0	0	0	0	0	1	3	34	180	338	217	69	48	52	56	57	47	36	25	15	8	3	1	0	0	0
243	0	0	0	0	0	0	0	1	4	42	222	402	242	85	36	37	39	37	29	21	14	7	4	1	0	0	0	0
241	0	0	0	0	0	0	0	1	4	44	229	398	228	56	26	25	25	22	16	11	7	3	1	0	0	0	0	0
239	0	0	0	0	0	0	0	1	3	39	196	327	179	41	18	16	15	12	8	5	3	1	1	0	0	0	0	0
237	0	0	0	0	0	0	0	1	3	28	139	223	118	26	11	9	8	6	4	2	1	1	0	0	0	0	0	0
235	0	0	0	0	0	0	0	2	18	82	127	64	14	6	5	4	3	1	1	1	0	0	0	0	0	0	0	0
233	0	0	0	0	0	0	0	1	9	40	60	29	7	3	2	1	1	0	0	0	0	0	0	0	0	0	0	0
231	0	0	0	0	0	0	0	4	17	23	11	3	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
229	0	0	0	0	0	0	0	2	6	7	3	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
227	0	0	0	0	0	0	0	1	2	2	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
225	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
223	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Digital image

Numbers are proportional to the intensity

Good for very slow links; rarely used anymore

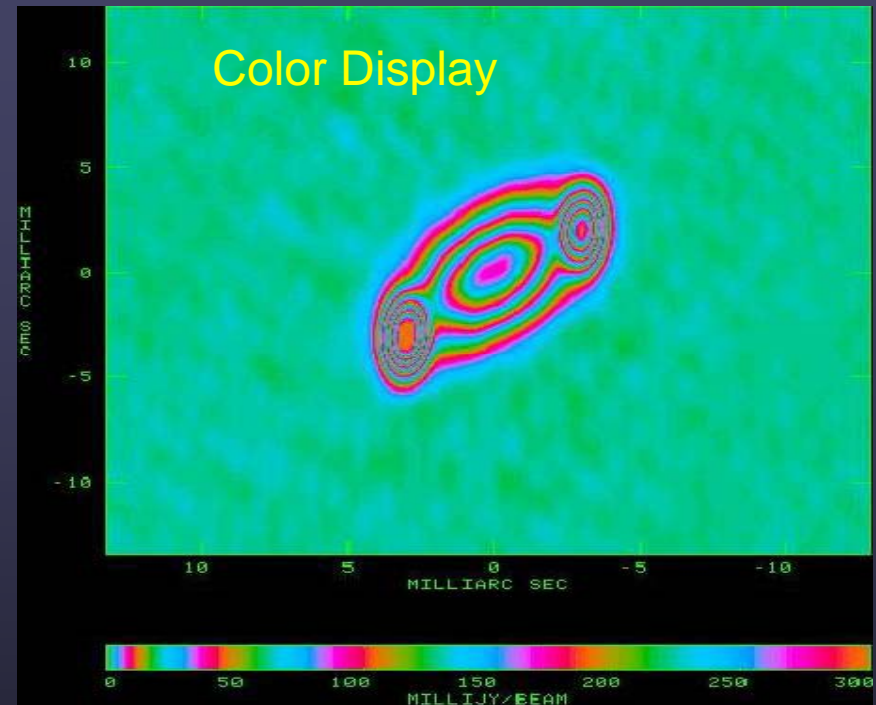
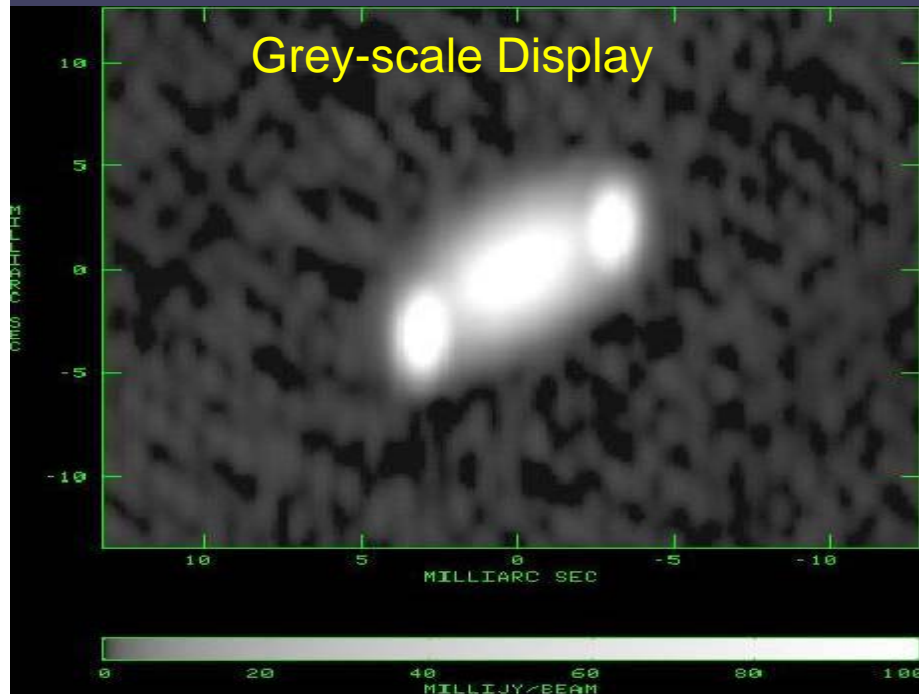
IMAGE DISPLAYS (1)



These plots are easy to reproduce and printed

- Contour plots give good representation of faint emission.
- Profile plots give a good representation of the bright emission and faint ripples.

IMAGE DISPLAYS (2)



TV-based displays are most useful and interactive:

- Grey-scale shows faint structure
 - but not good for high dynamic range and somewhat unbiased view of source
- Color displays more flexible; e.g. pseudo contours

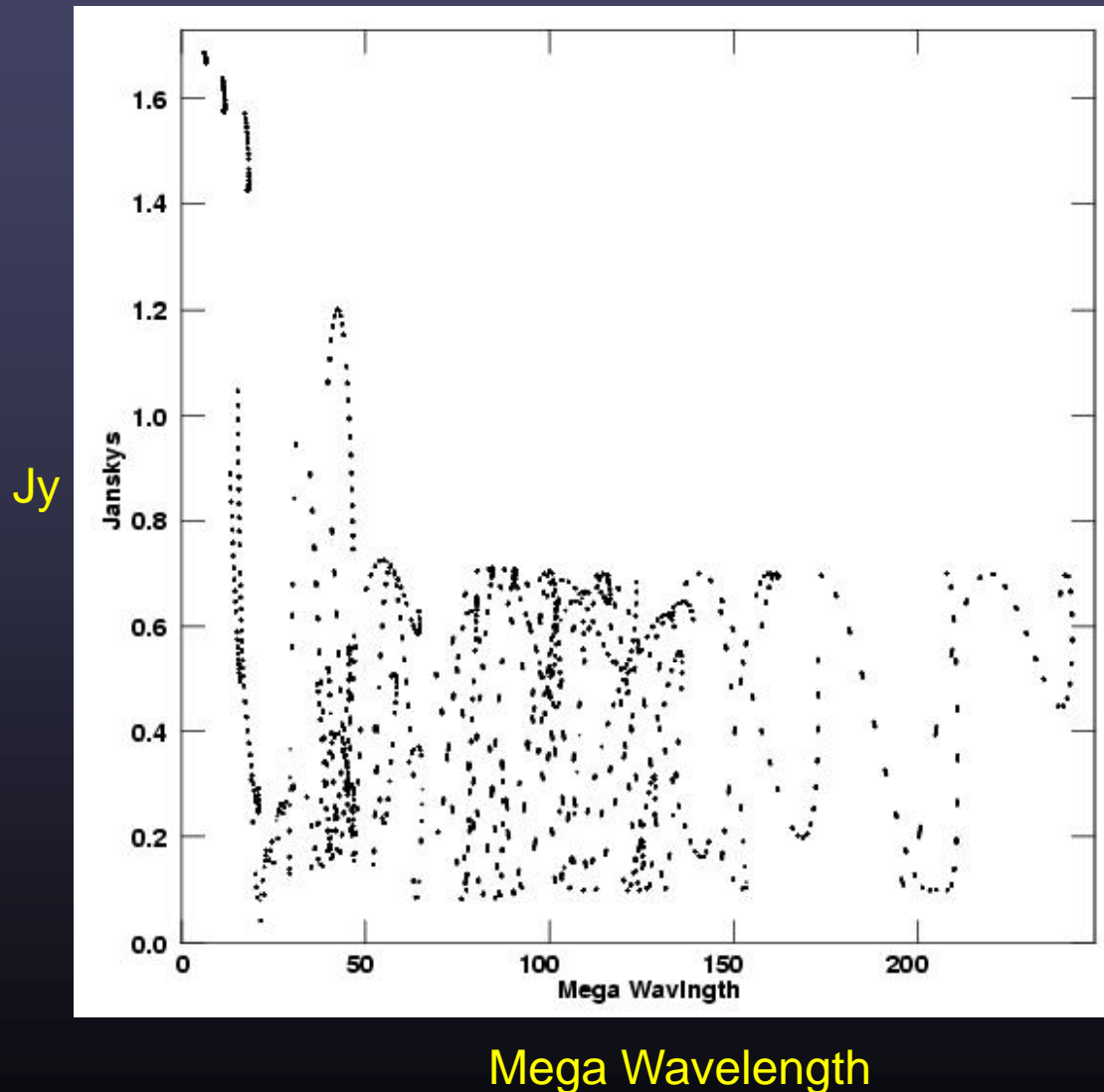
DATA DISPLAYS(1)

List of u-v Data

Source= J0121+11		Freq= 8.434858511		Sort= TB		1 RR				
Vis #	IAT	Ant	Su	Fq	U(klam)	V(klam)	W(klam)	Amp	Phas	Wt
2191	0/22:35:08.22	5- 6	1	0	94220	23776	100371	0.614	-16	1.0000
3971	0/22:43:43.34	5- 6	1	0	97659	24517	96844	0.508	-13	1.0000
6431	0/23:07:05.15	5- 6	1	0	106307	26661	86632	0.154	17	1.0000
6611	0/23:07:14.98	5- 6	1	0	106364	26677	86557	0.152	17	1.0000
6791	0/23:07:24.81	5- 6	1	0	106421	26692	86483	0.150	18	1.0000
6971	0/23:07:34.64	5- 6	1	0	106477	26708	86408	0.148	19	1.0000
7151	0/23:07:44.47	5- 6	1	0	106534	26724	86333	0.146	19	1.0000
7331	0/23:07:54.30	5- 6	1	0	106591	26739	86259	0.144	20	1.0000
7511	0/23:15:06.84	5- 6	1	0	109027	27438	82930	0.101	74	1.0000
7691	0/23:15:16.67	5- 6	1	0	109081	27454	82854	0.101	75	1.0000
7871	0/23:15:26.50	5- 6	1	0	109135	27470	82777	0.102	77	1.0000
8051	0/23:15:36.33	5- 6	1	0	109189	27486	82701	0.102	78	1.0000
8231	0/23:15:46.16	5- 6	1	0	109243	27502	82624	0.103	79	1.0000
8411	0/23:15:55.99	5- 6	1	0	109297	27518	82547	0.104	81	1.0000
9701	0/23:31:02.36	5- 6	1	0	114020	29035	75322	0.260	134	1.0000
9791	0/23:31:06.29	5- 6	1	0	114040	29042	75290	0.261	134	1.0000
10301	0/23:31:29.88	5- 6	1	0	114156	29082	75098	0.266	134	1.0000
10861	0/23:39:02.08	5- 6	1	0	116320	29863	71379	0.348	139	1.0000
10951	0/23:39:06.01	5- 6	1	0	116339	29870	71346	0.348	139	1.0000
11171	0/23:39:15.84	5- 6	1	0	116384	29887	71264	0.350	139	1.0000

Very primitive display, but sometimes worth-while: e.g. , can search on e.g. Amp > 1.0, or large Wt. Often need precise times in order to flag the data appropriately.

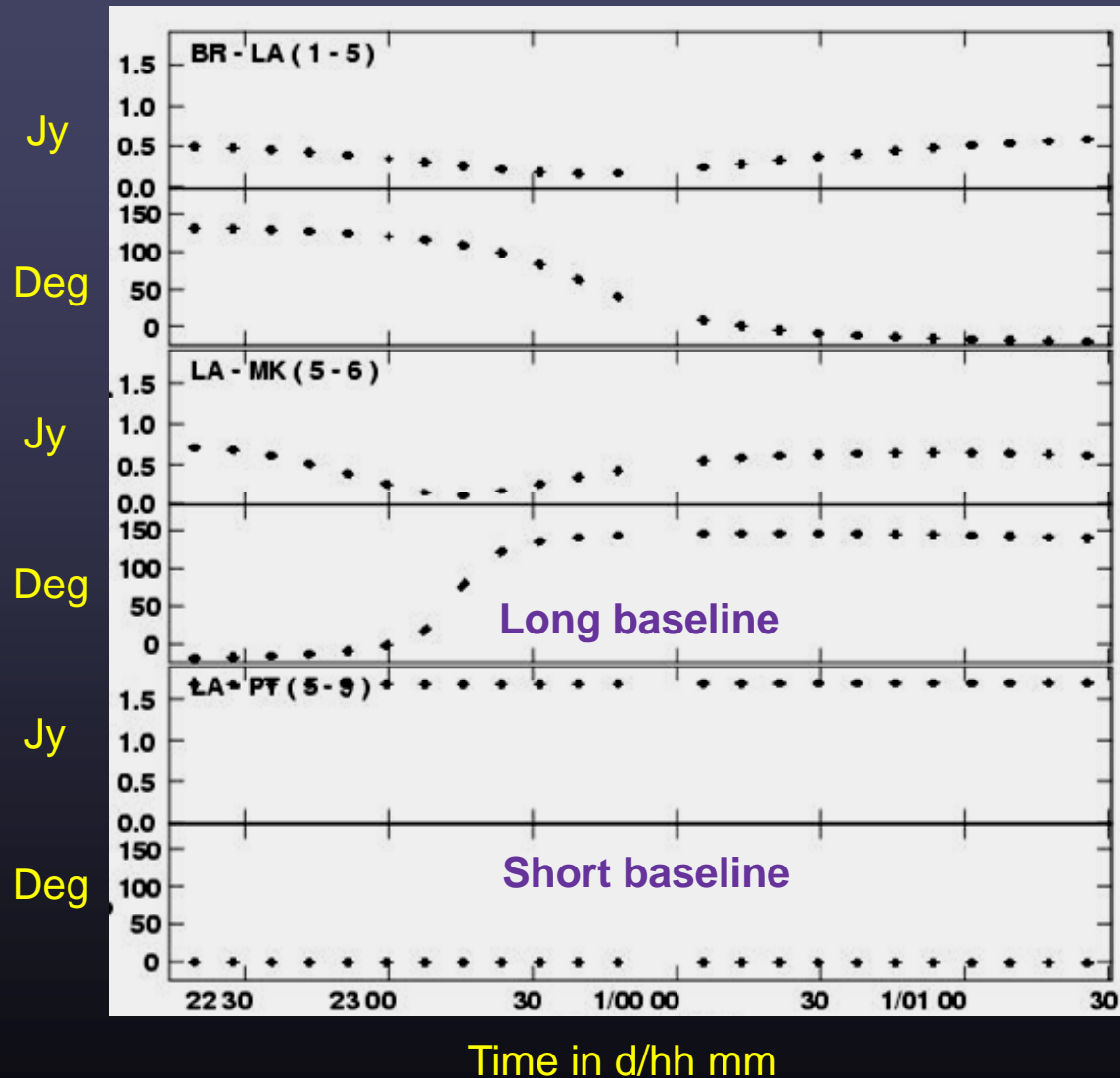
DATA DISPLAYS(2)



Visability amplitude vs. u-v distance plot

- General trend of data
- Useful for strong sources
- This is model from image showed earlier
 - Large fuzzy structure caused rise in flux towards short spacings
 - Oscillations at longer spacings suggest close double

DATA DISPLAYS(3)

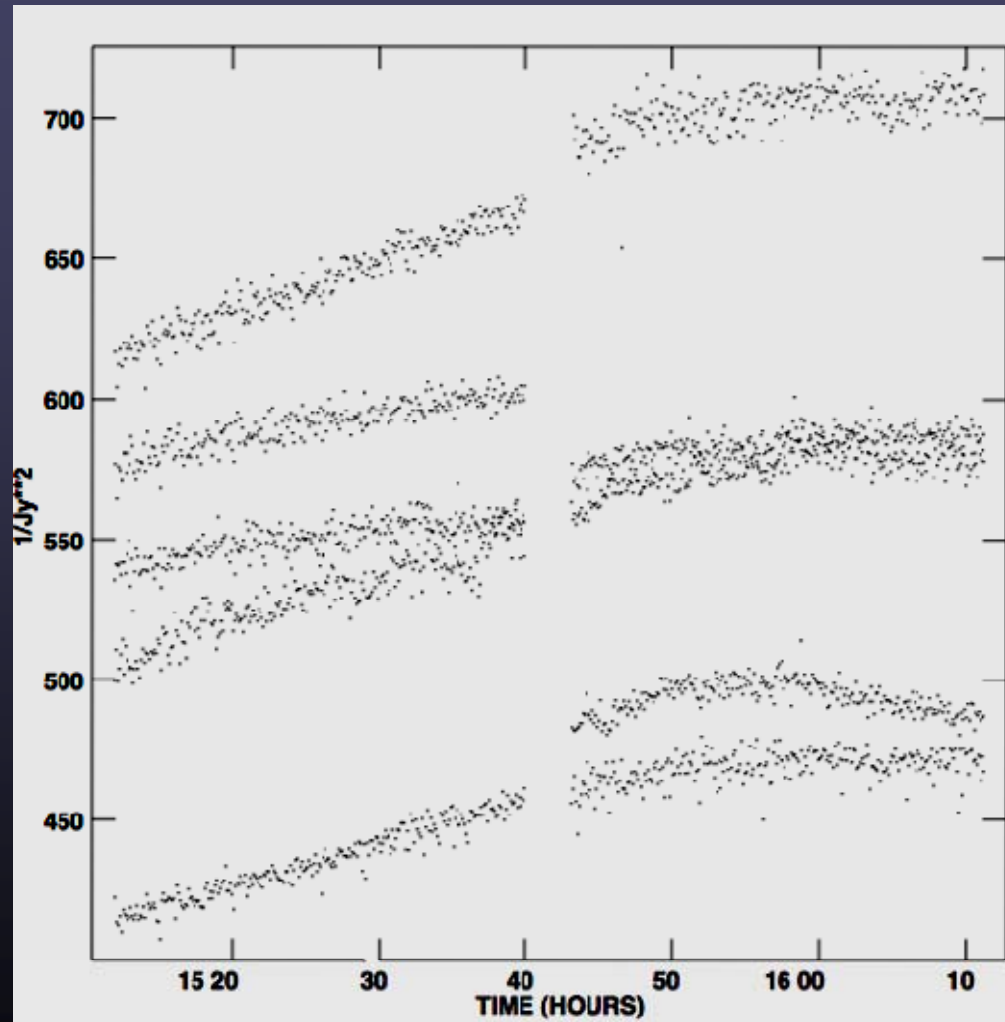


Amplitude and phase vs. time on various baselines

- Good for determining the continuity of the data
- Should be relatively smooth with time
- Outlier are obvious

DATA DISPLAYS(4)

Weights of antennas 4 with 5,6,7,8,9



- All u-v data points have a weight.
- The weight depends on the antenna sensitivity, measured during the observations
- The amplitude calibration values also modify the weights.
- Occasionally the weight of the points become very large, often caused by subtle software bugs.
- A large discrepant weight causes the same image artifacts as a large discrepant visibility value.
- Check weights to make sure they are reasonable.

IMAGE PLANE OR DATA (U-V) PLANE INSPECTION?

Errors obey Fourier transform relationship

- Narrow feature in uv plane \leftrightarrow wide feature in image plane
- Wide feature in uv plane \leftrightarrow narrow feature in image plane
 - **Note: easier to spot narrow features**
- Orientations are orthogonal
- Data uv amplitude errors \leftrightarrow symmetric image features
- Data uv phase errors \leftrightarrow asymmetric image features
- An obvious defect may be hardly visible in the transformed plane
- A small, almost invisible defect may become very obvious in the transformed plane

GOLDEN RULES OF FINDING ERRORS

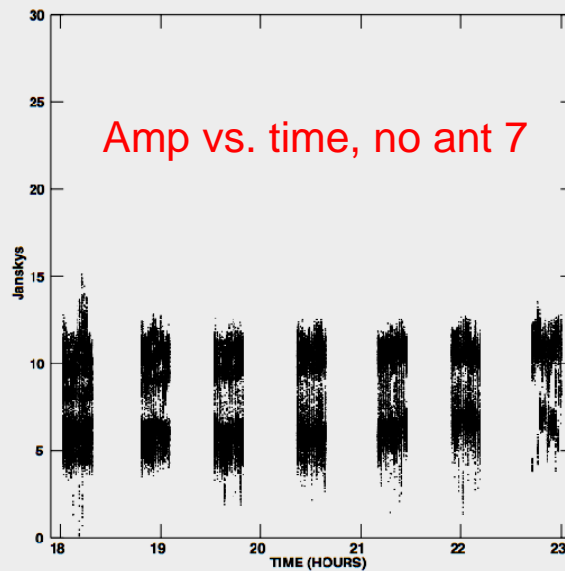
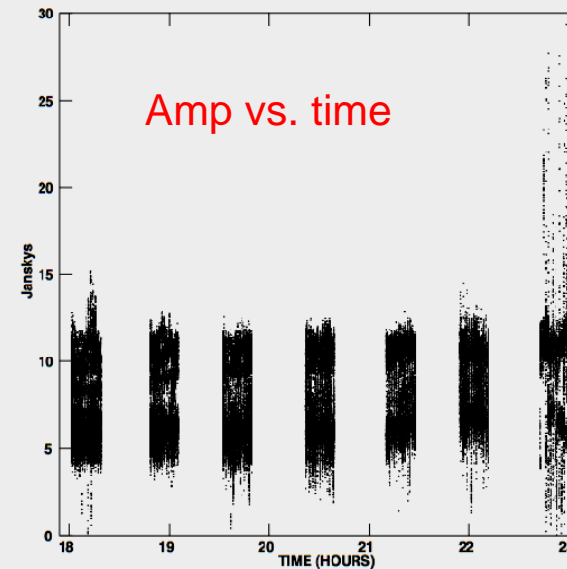
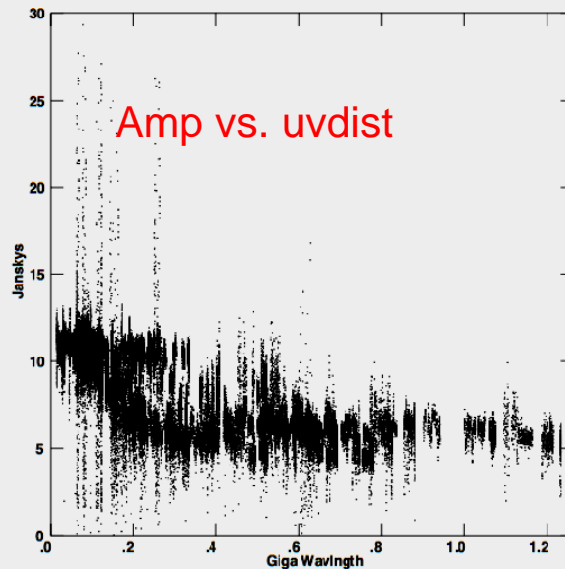
- Obvious outlier data (u-v) points:
 - 100 bad points in 100,000 data points gives an 0.1% image error (unless the bad data points are 1 million Jy)
 - LOOK AT DATA to find gross problem (you'd be hard pressed to find in the image plane other than a slight increase in noise)
- Persistent small data errors are a bigger problem:
 - e.g. a 5% antenna gain calibration error is difficult to see in (u-v) data (not an obvious outlier), but will produce a 1% effect in image with specific characteristics (more later).
 - USE IMAGE to discover problem
- Non-data problems:
 - Perfect data but unstable algorithms. Common but difficult to discern

ERROR RECOGNITION IN THE U-V PLANE

Editing obvious errors in the u-v plane

- Mostly consistency checks assume that the visibility cannot change much over a small change in u-v spacing
- Also, double-check gains and phases from calibration processes. These values should be relatively stable.

VISIBILITY AMPLITUDE PLOTS



Amp vs. uvdist shows outliers

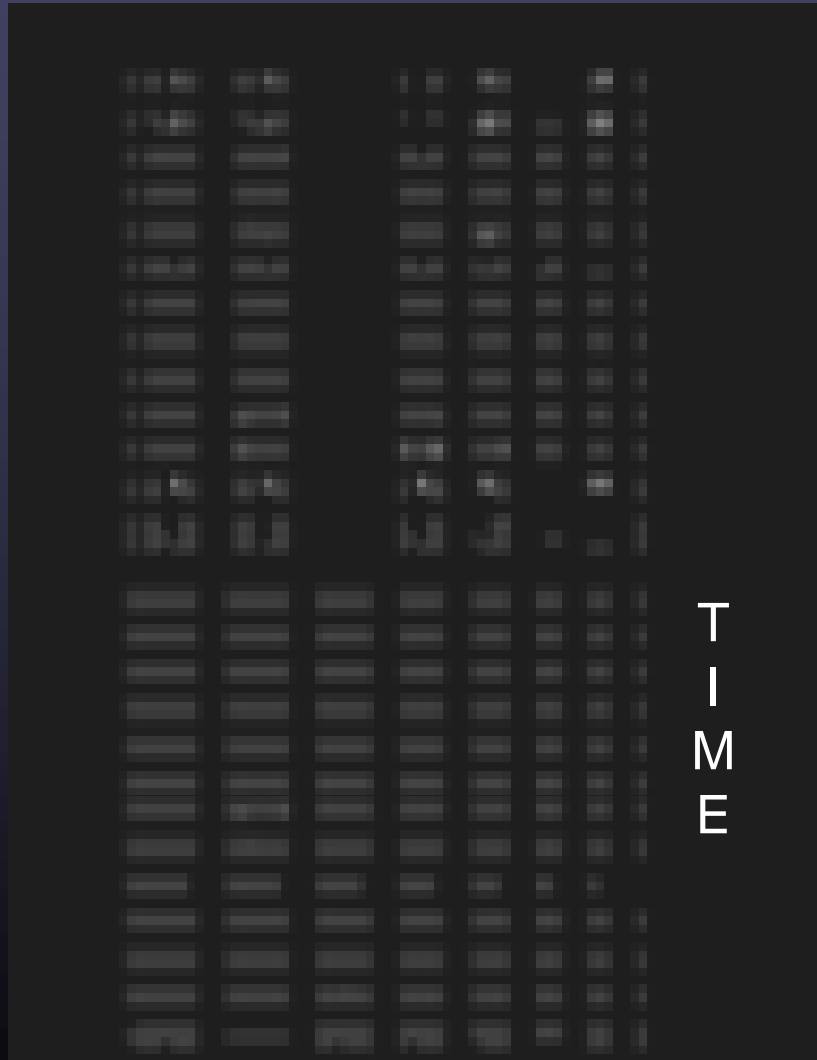
Amp vs. time shows outliers in last scan

Amp vs. time without ant 7 should good data

(3C279 VLBA data at 43 GHz)

VISIBILITY AMPLITUDE RASTERS

BASELINE
Ant 1 2 3 4 5 6 7 8



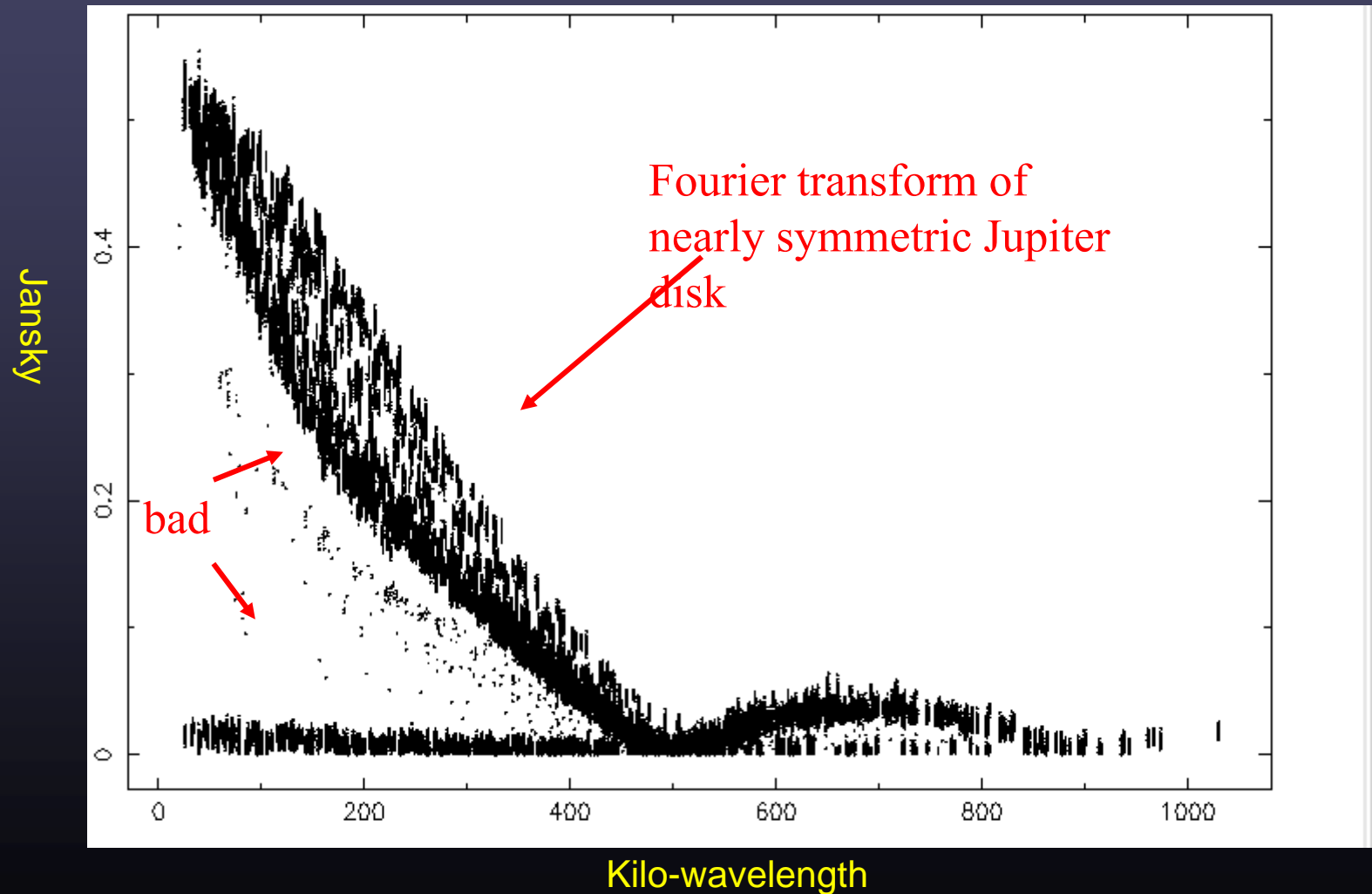
(Last two scans from last slide)

Use AIPS task TVFLG or CASA viewer

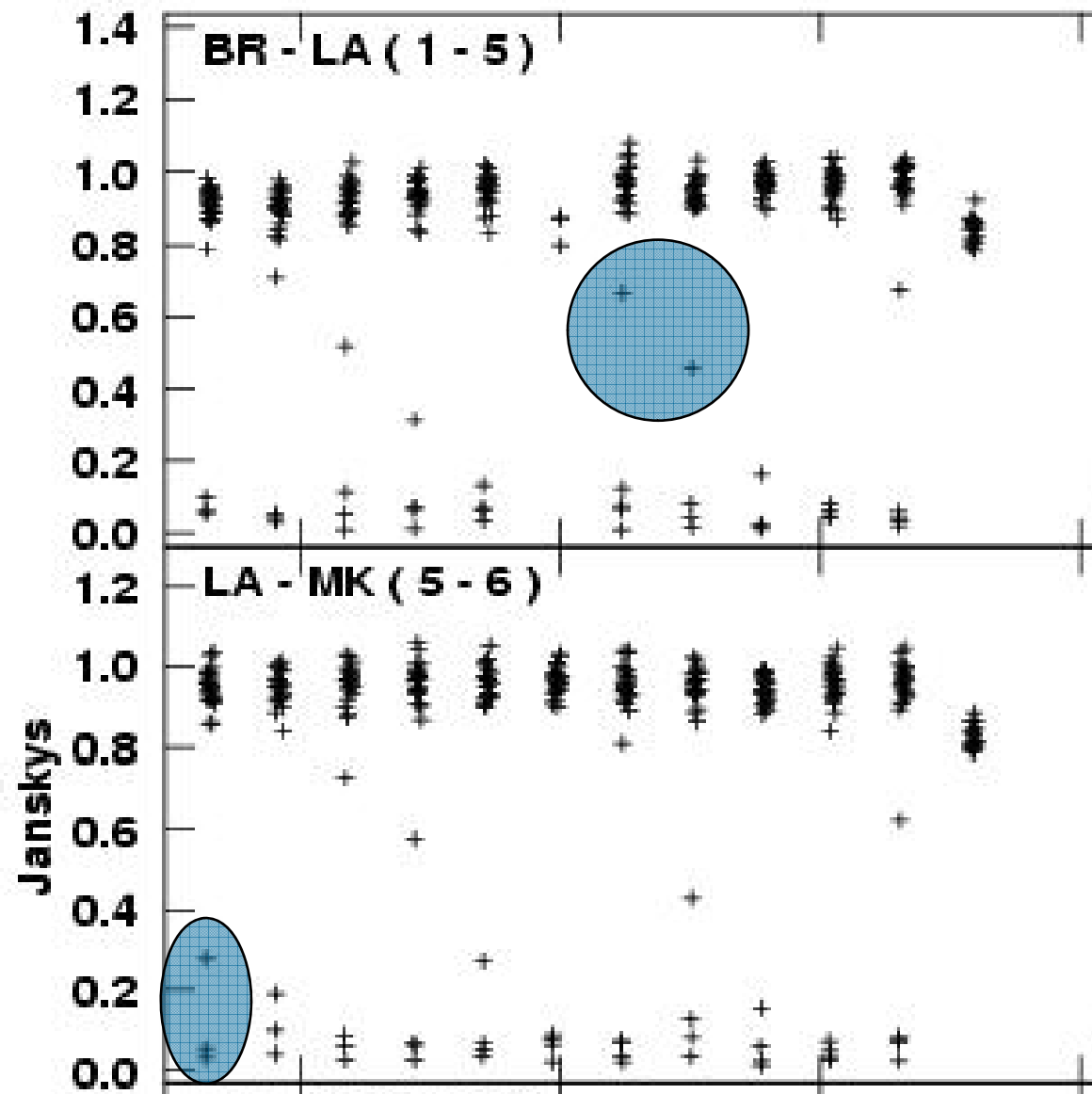
- Raster scan of baseline versus time immediately shows where the bad data are
- Pixel range is 5 to 20 Jy
- Bad data can be flagged with an interactive clipping control

Example Edit (2)

AIPS WIPER or CASA plotms



Drop-outs at Scan Beginnings



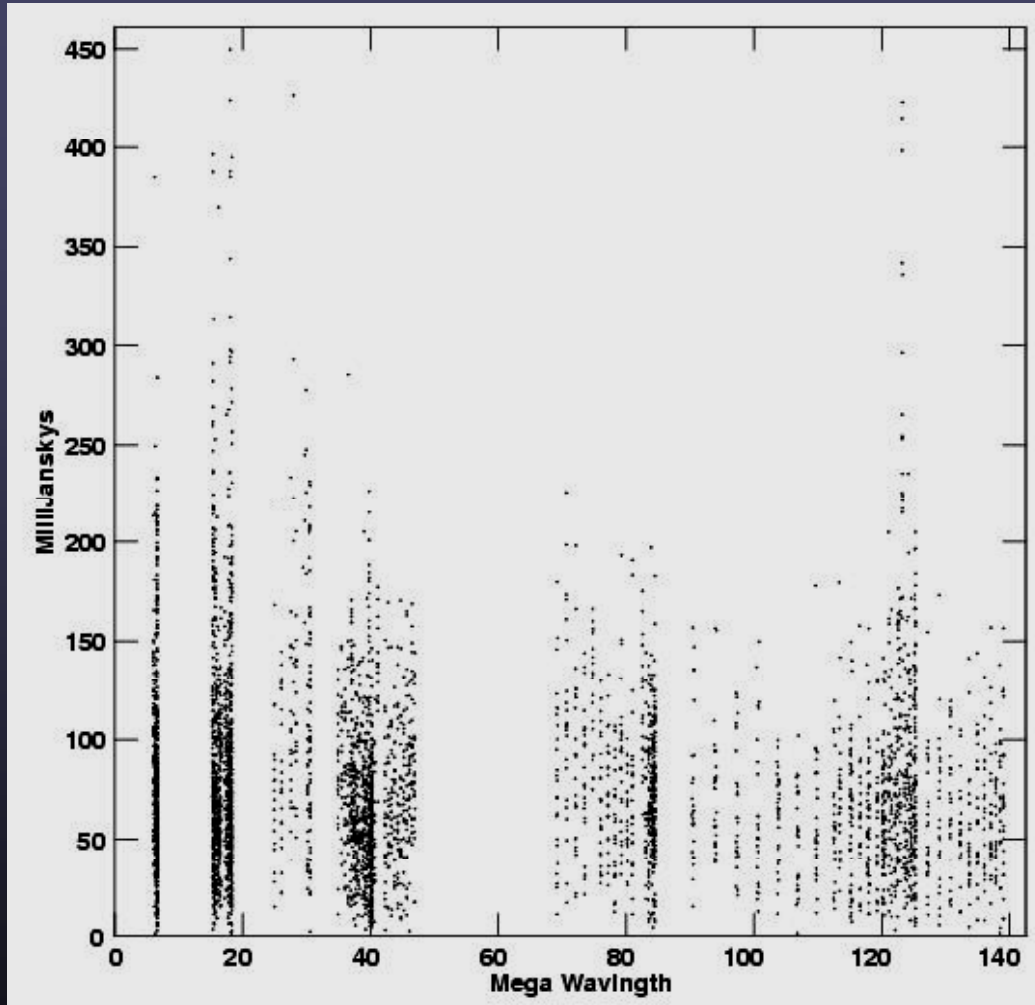
Often the first few points of a scan are low. E.g. antenna not on source.

Software can remove these points (aips,casa 'quack')

Flag extension:

Should flag all sources in the same manner even though you cannot see dropout for weak sources

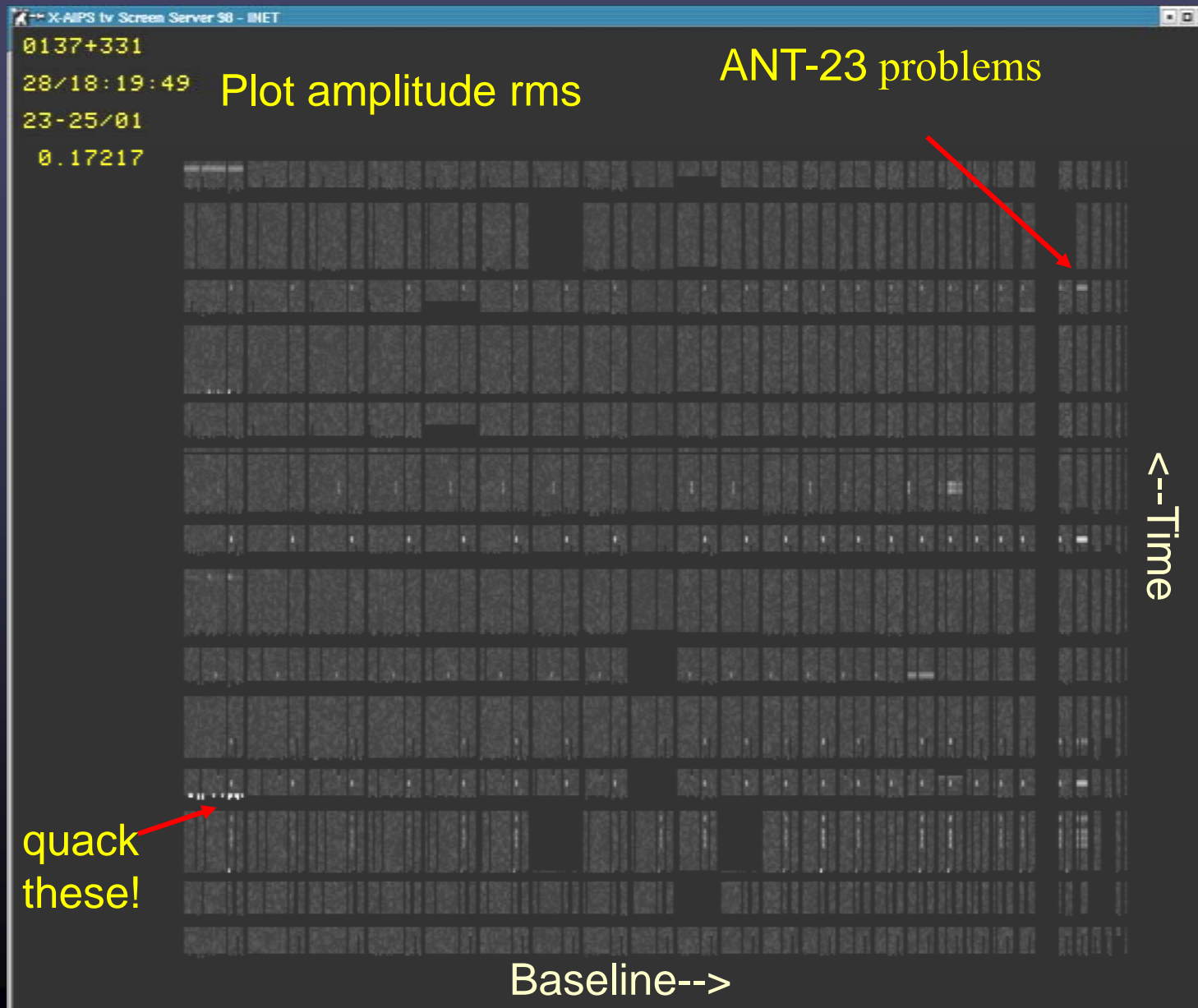
Editing Noise-dominated Sources



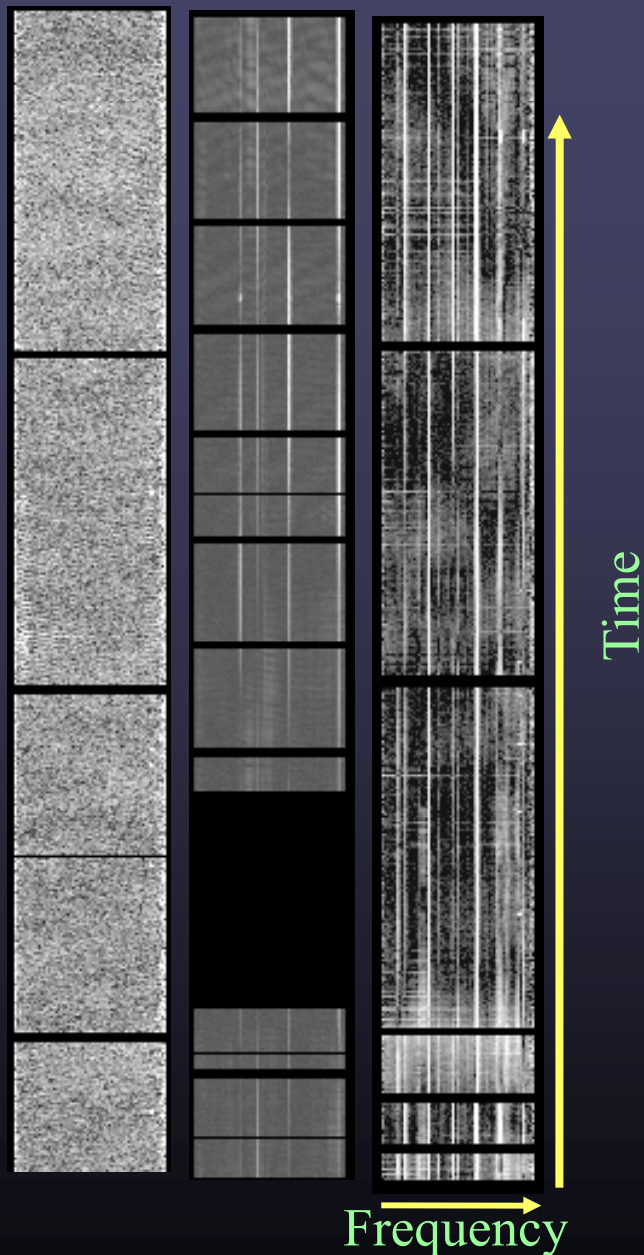
No source structure
information is detected.
Noise dominated.

All you can do is remove
outlier points above
0.3 Jy. Precise level
not important as long
as large outliers
removed.

USING TVFLG (VIEWER) DISPLAY on a source



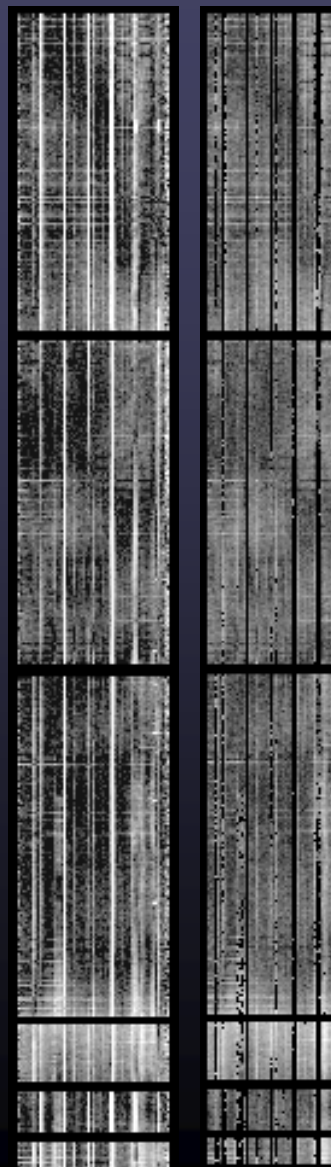
35 km 12 km 3 km baseline



AIPs: SPFLG

RFI Excision

before after



RFI environment worse on short baselines

Several 'types': narrow band, wandering, wideband, ...

Wideband interference hard for automated routines

AIPS tasks FLGIT, FLAGR, and CASA flagdata, mode='rfi'

Automation is crucial for WIDAR (wide band, lots of data)

ERROR RECOGNITION IN THE IMAGE PLANE

Some Questions to ask:

Noise properties of image:

Is the rms noise about that expected from integration time?

Is the rms noise much larger near bright sources?

Are there non-random noise components (faint waves and ripples)?

Funny looking Structure:

Non-physical features; stripes, rings, symmetric or anti-symmetric

Negative features well-below 4σ noise

Does the image have characteristics in the dirty beam?

Image-making parameters:

Is the image big enough to cover all significant emission?

Is cell size too large or too small? ~ 4 points per beam okay

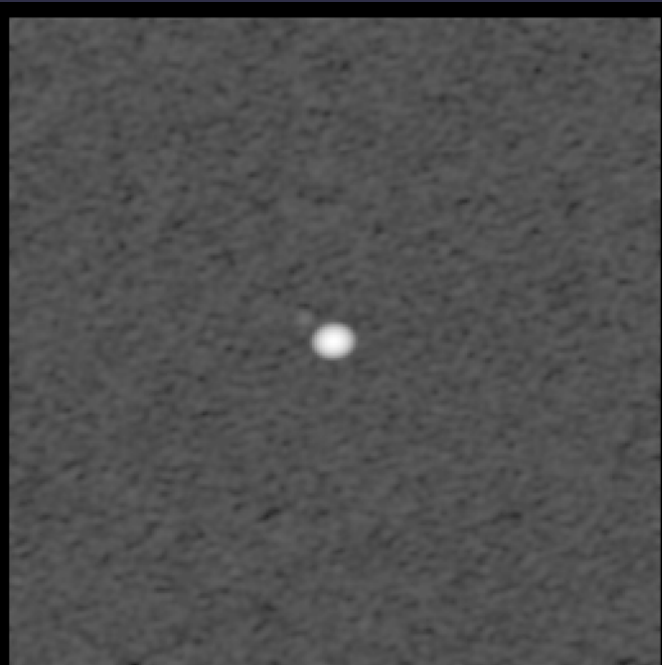
Is the resolution too high to detect most of the emission?

EXAMPLE 1

Data bad over a short period of time

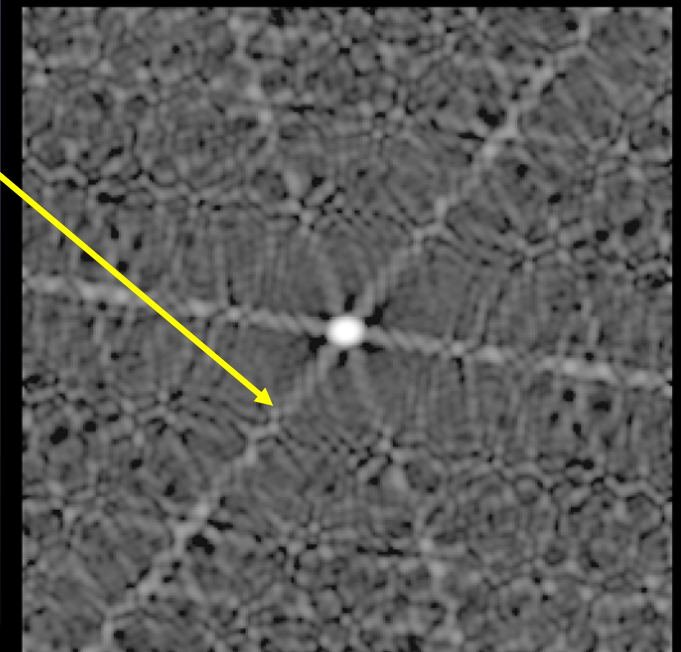
Results for a point source using VLA. 13-5min observations over 10 hr.
Images shown after editing, calibration and deconvolution.

no errors:
max 3.24 Jy
rms 0.11 mJy



10% amp error for all
antennas for 1 time period
rms 2.0 mJy

6-fold symmetric
pattern due to
VLA "Y".
Image has
properties of dirty
beam.

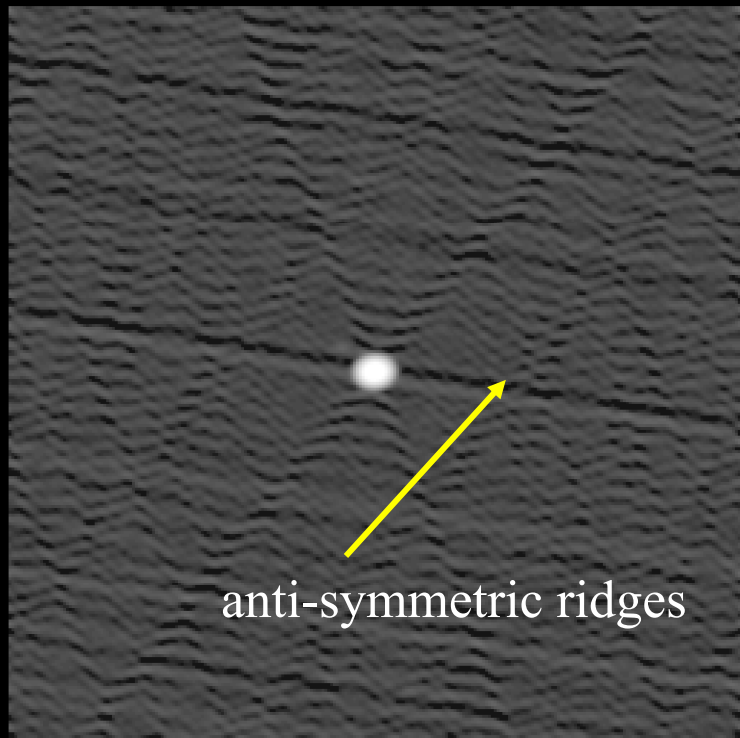


EXAMPLE 2

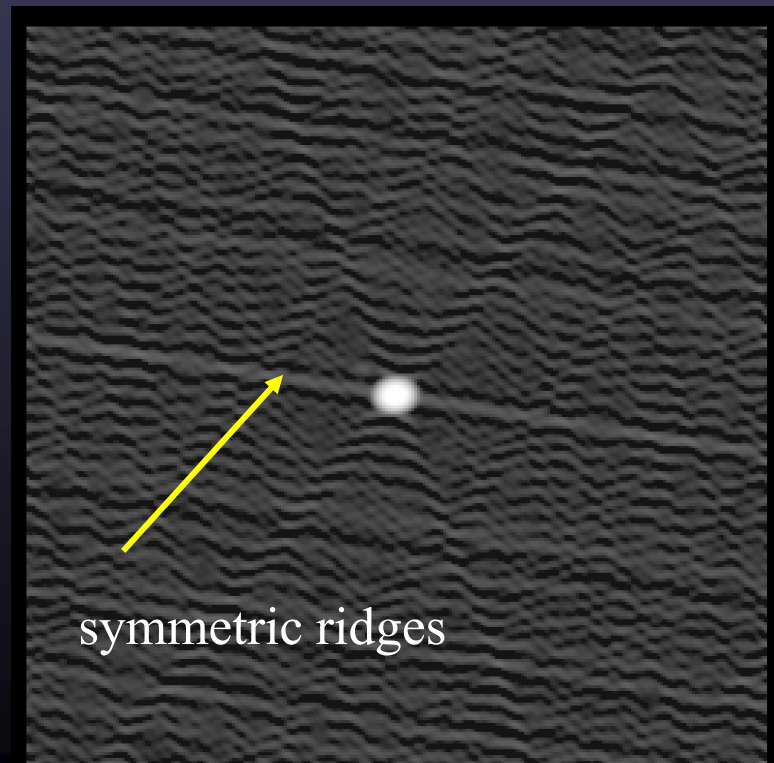
Short burst of bad data

Typical effect from one bad antenna

10 deg ***phase error*** for
one antenna at one time
rms 0.49 mJy



20% ***amplitude error*** for
one antenna at one time
rms 0.56 mJy

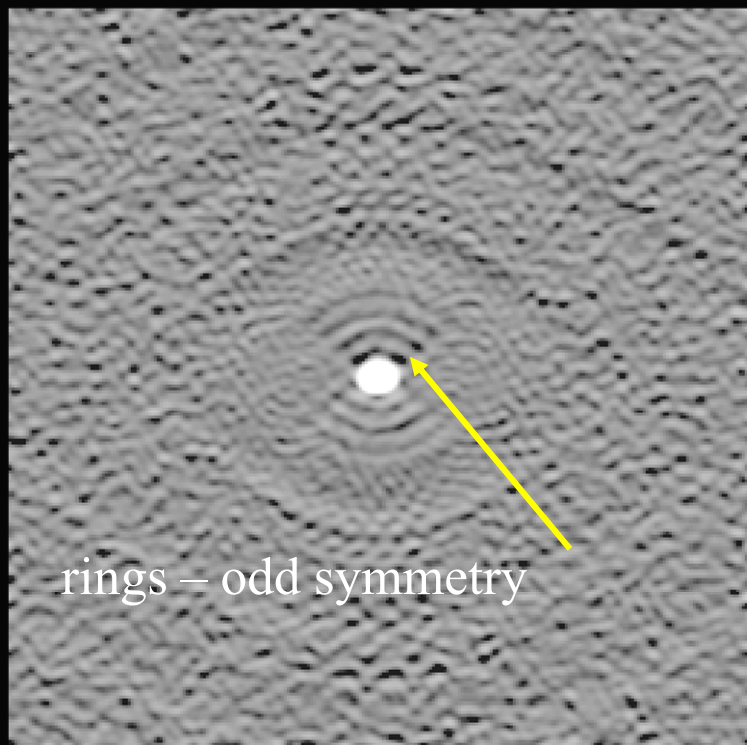


EXAMPLE 3

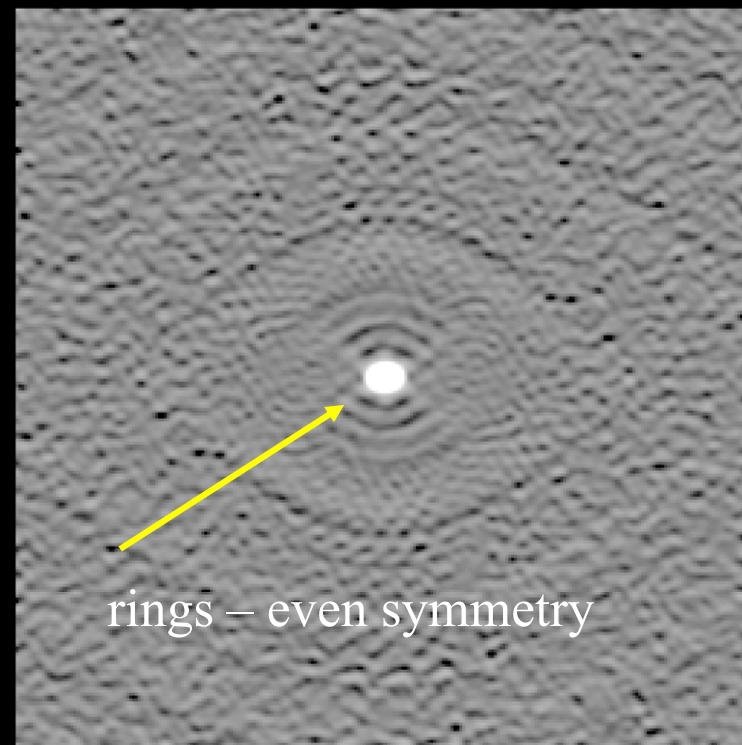
Persistent errors over most of observations

NOTE: 10 deg phase error to 20% amplitude error
cause similar sized artifacts

10 deg **phase error** for
one antenna all times
rms 2.0 mJy



20% **amp error** for
one antenna all times
rms 2.3 mJy



EXAMPLE 4

Spurious Correlator Offset Signals

Occasionally correlators produce ghost signals or cross talk signals
Occurred during change-over from VLA to EVLA system

Symptom: Garbage near phase center, dribbling out into image

Image with correlator offsets

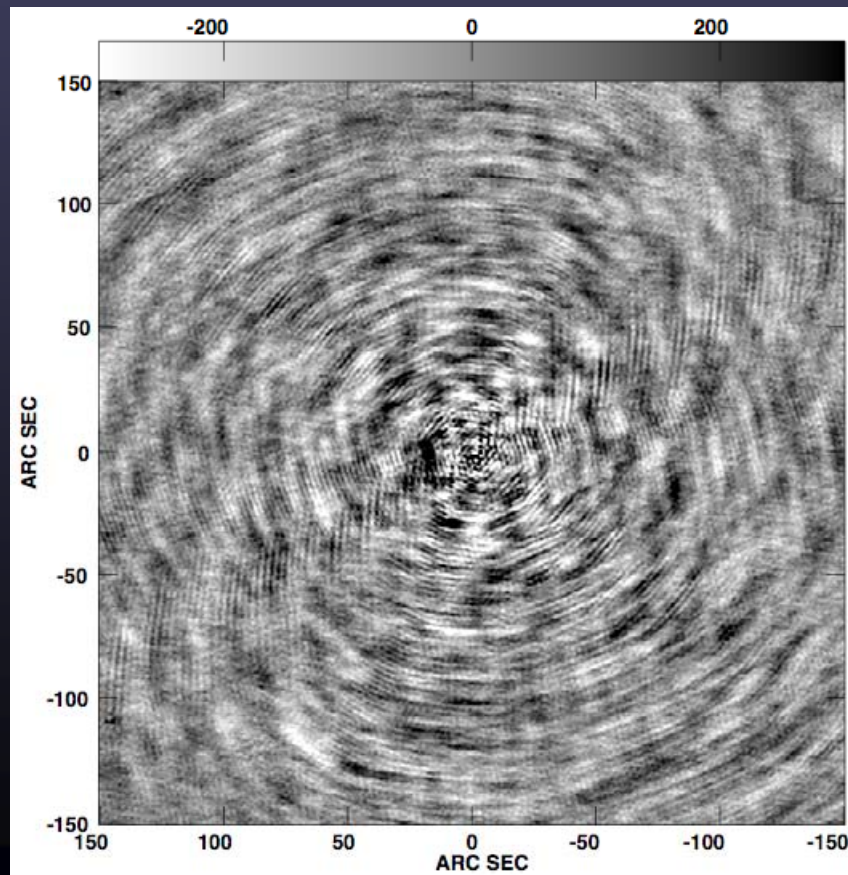
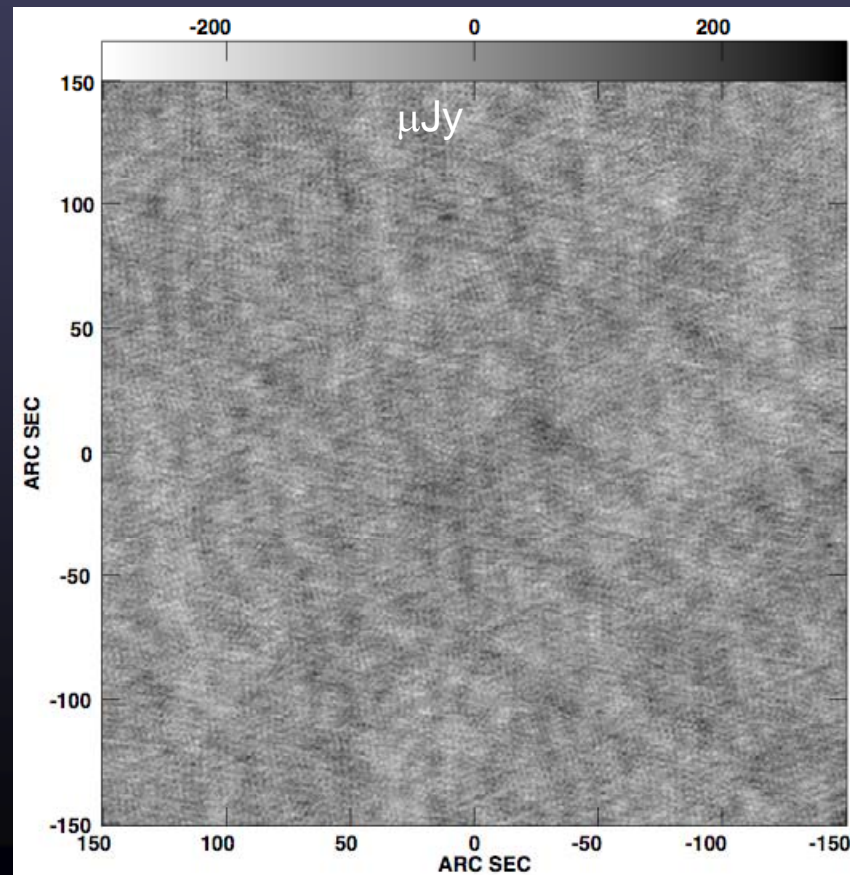
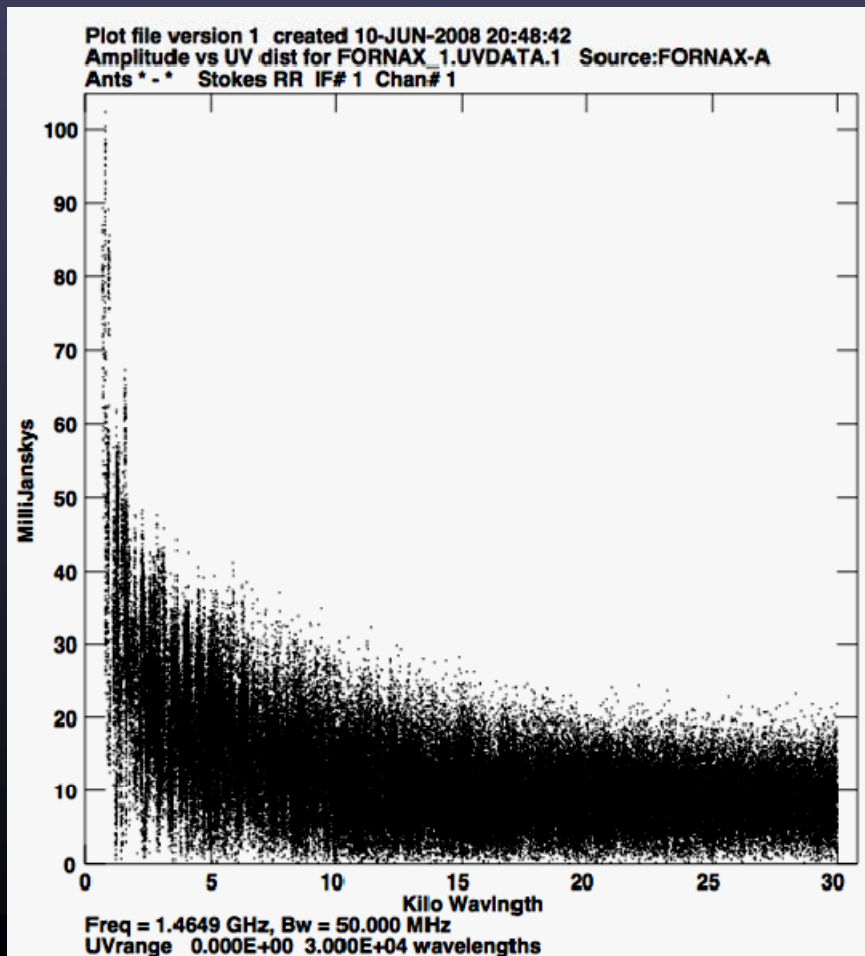


Image after correlation of offsets



DECONVOLUTION ERRORS

Even if the data are perfect, image errors and uncertainties will occur because the (u-v) coverage is not adequate to map the source structure.



The extreme rise of visibility at the short spacings makes it impossible to image the extended structure. You are better of imaging the source with a cutoff below about 2 kilo-wavelengths

Get shorter spacing or single-dish data

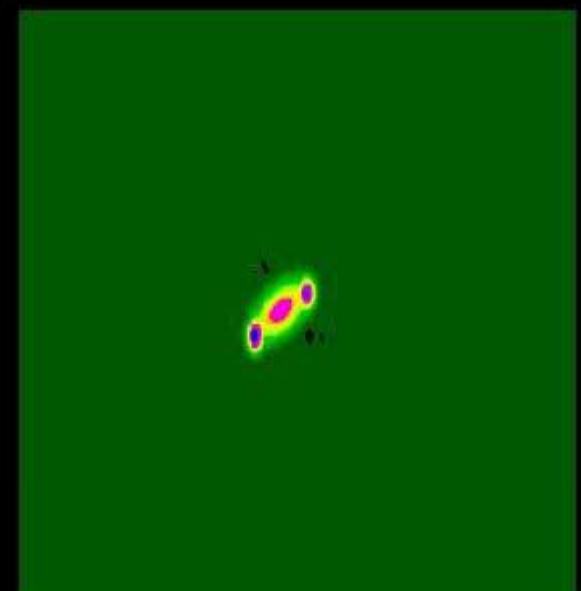
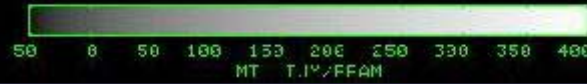
DIRTY IMAGE and BEAM (point spread function)



Dirty Beam



Dirty Image



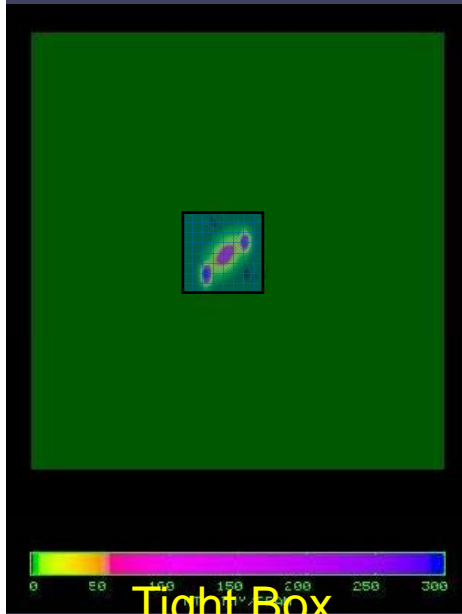
Source Model



The dirty beam has large, complicated side-lobe structure.
It is often difficult to recognize any details on the dirty image.
An extended source exaggerates the side-lobes.

5% in dirty beam becomes 20% for extended source

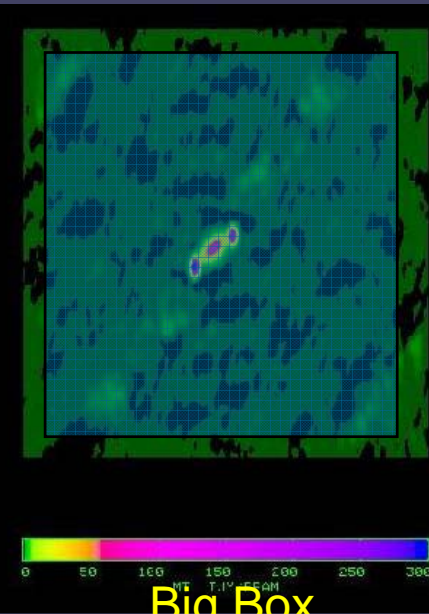
CLEANING WINDOW SENSITIVITY



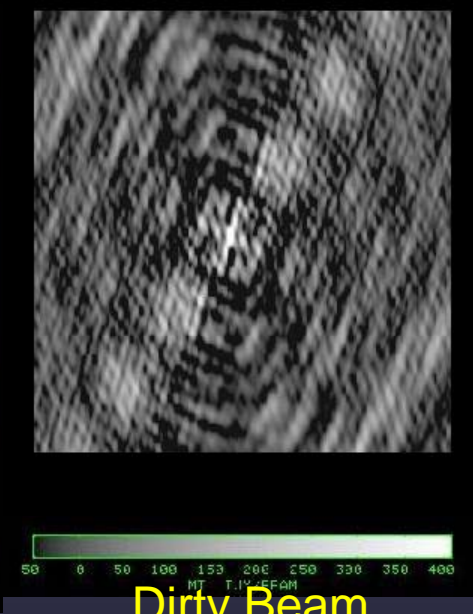
One small clean box



One clean box around all emission



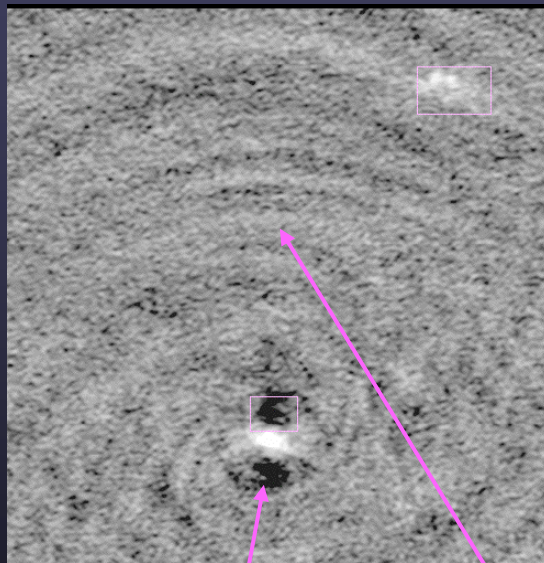
Clean entire inner map quarter



Make box as small as possible to avoid cleaning noise interacting with sidelobes

How Deep to Clean?

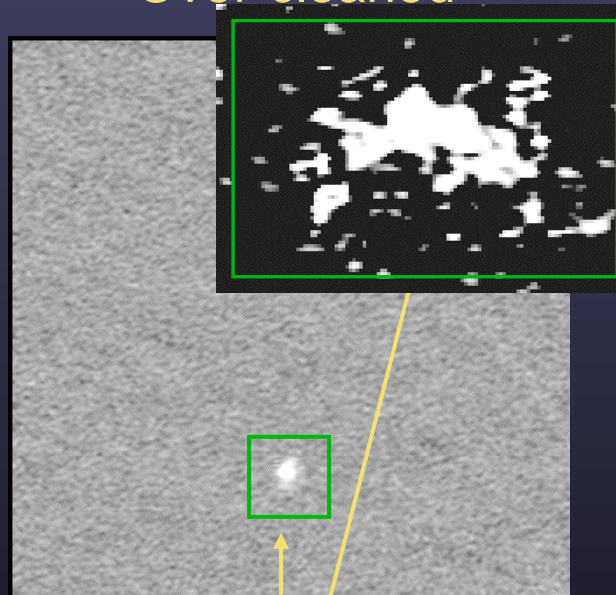
Under-cleaned



Emission from
second source sits
atop a negative "bowl"

Residual sidelobes
dominate the noise

Over-cleaned



Regions within
clean boxes
appear "mottled"

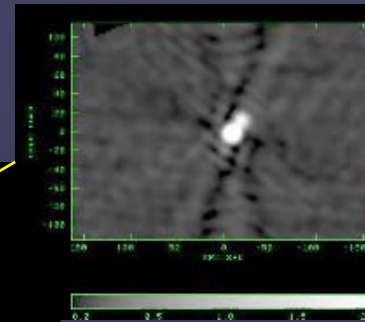
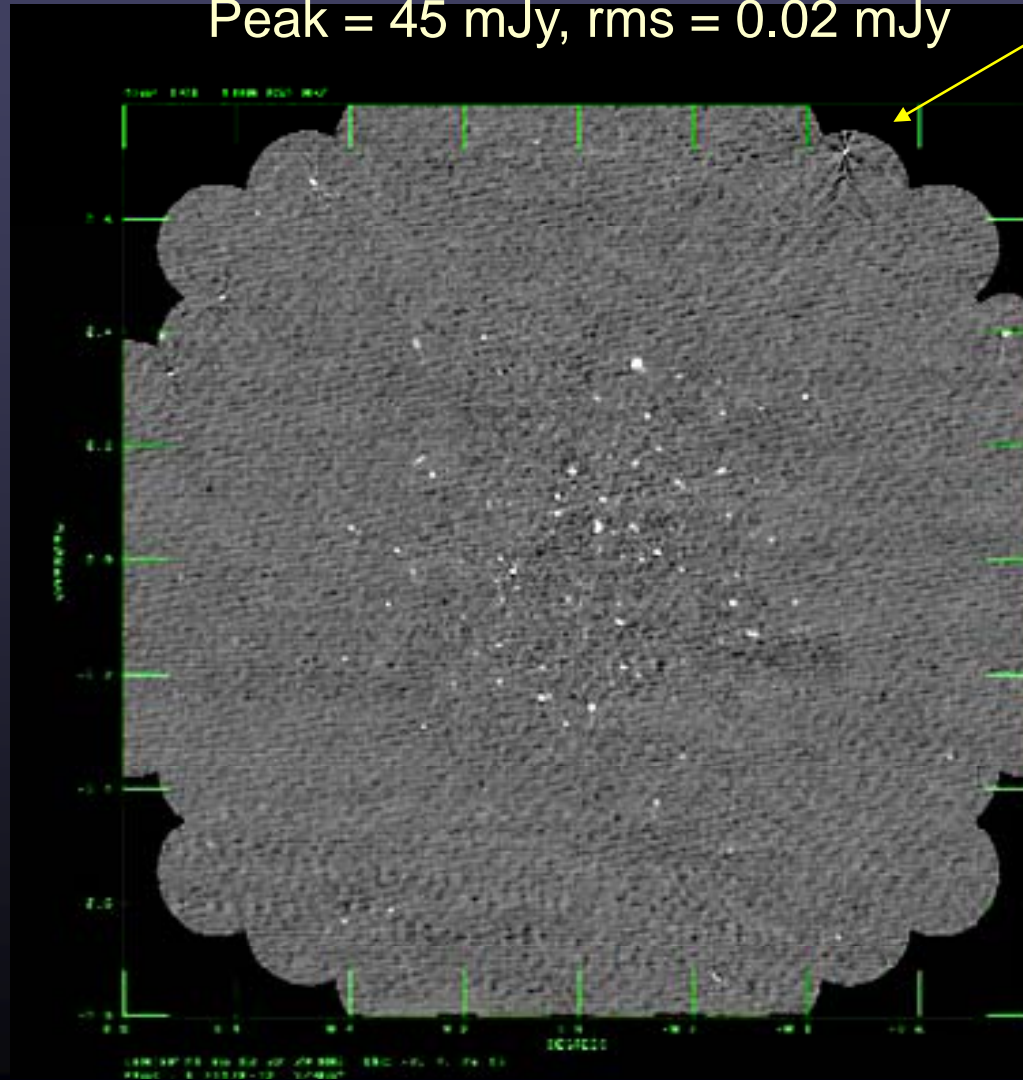
Properly cleaned



Background is thermal
noise-dominated;
no "bowls" around
sources.

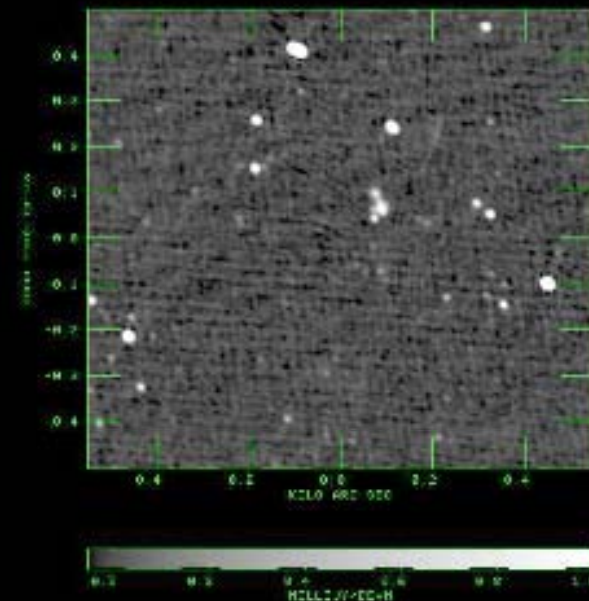
FINDING HIDDEN BAD DATA

VLA observation of Chandra
Deep Field South
Peak = 45 mJy, rms = 0.02 mJy

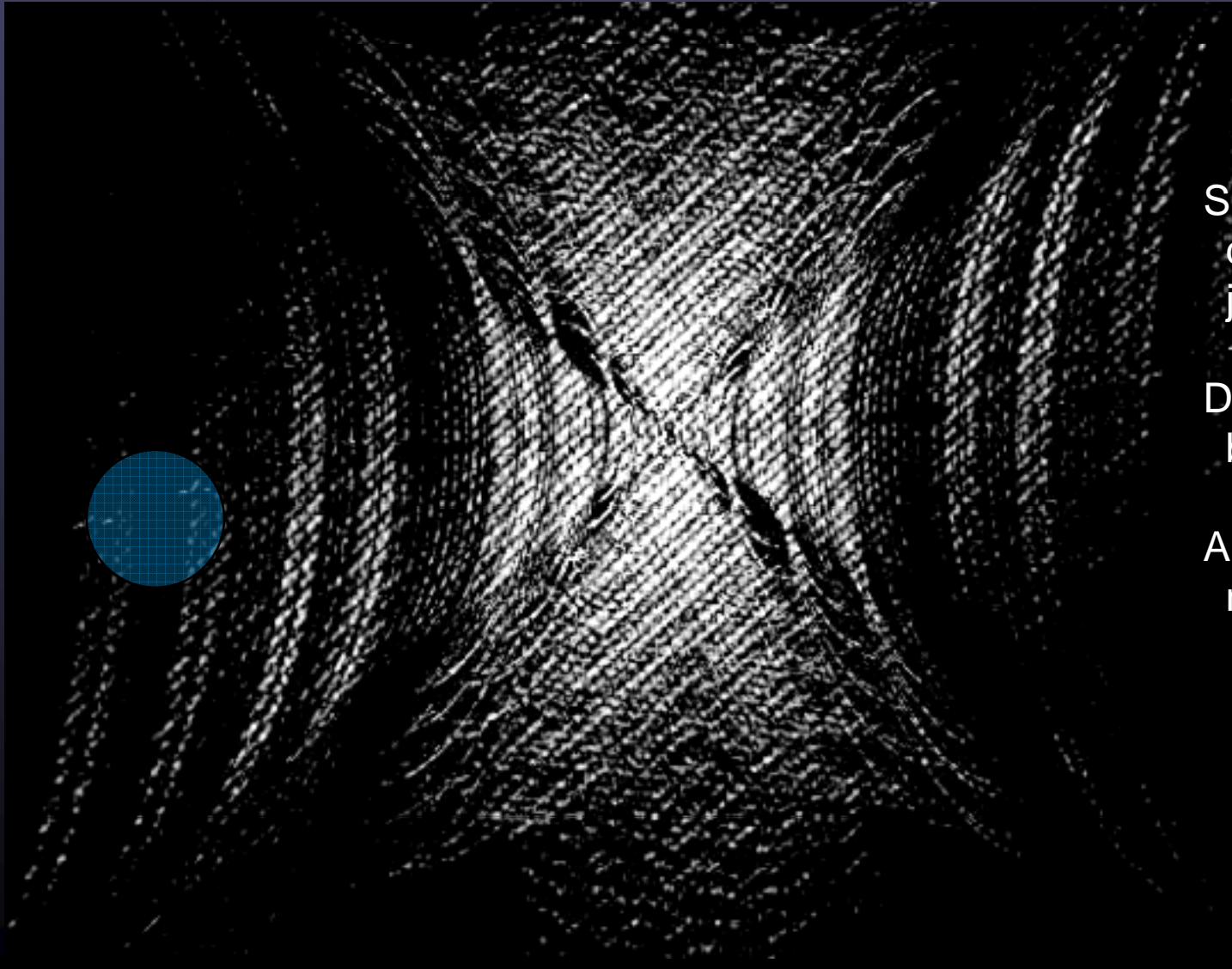


Source to NE in first
Primary beam
sidelobe

Center of Field



Fourier Transform Dirty Image

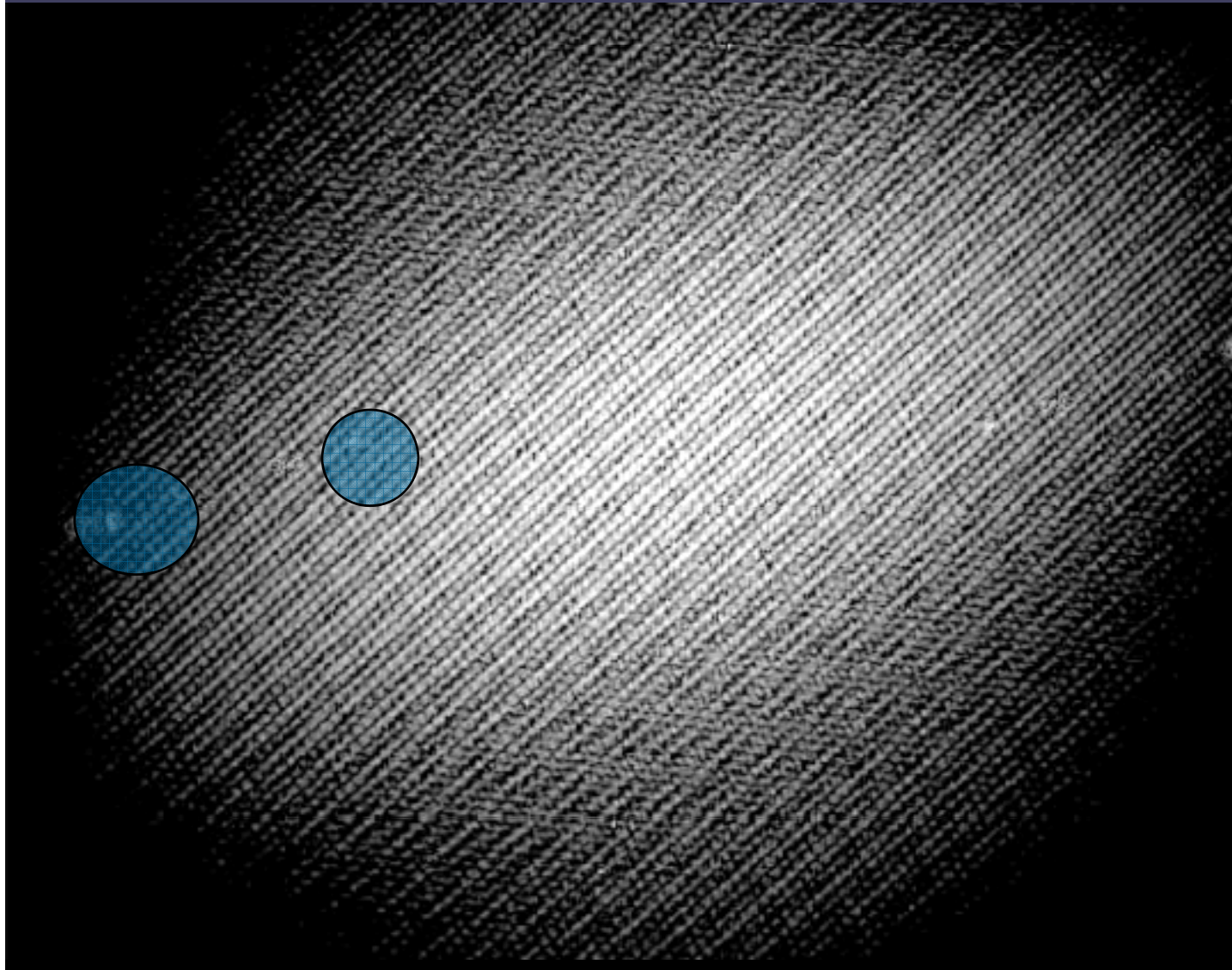


Shows the u - v
data as gridded
just before imaging

Diagonal lines caused
by structure in field

A few odd points are
not very noticeable

Fourier Transform Clean Image

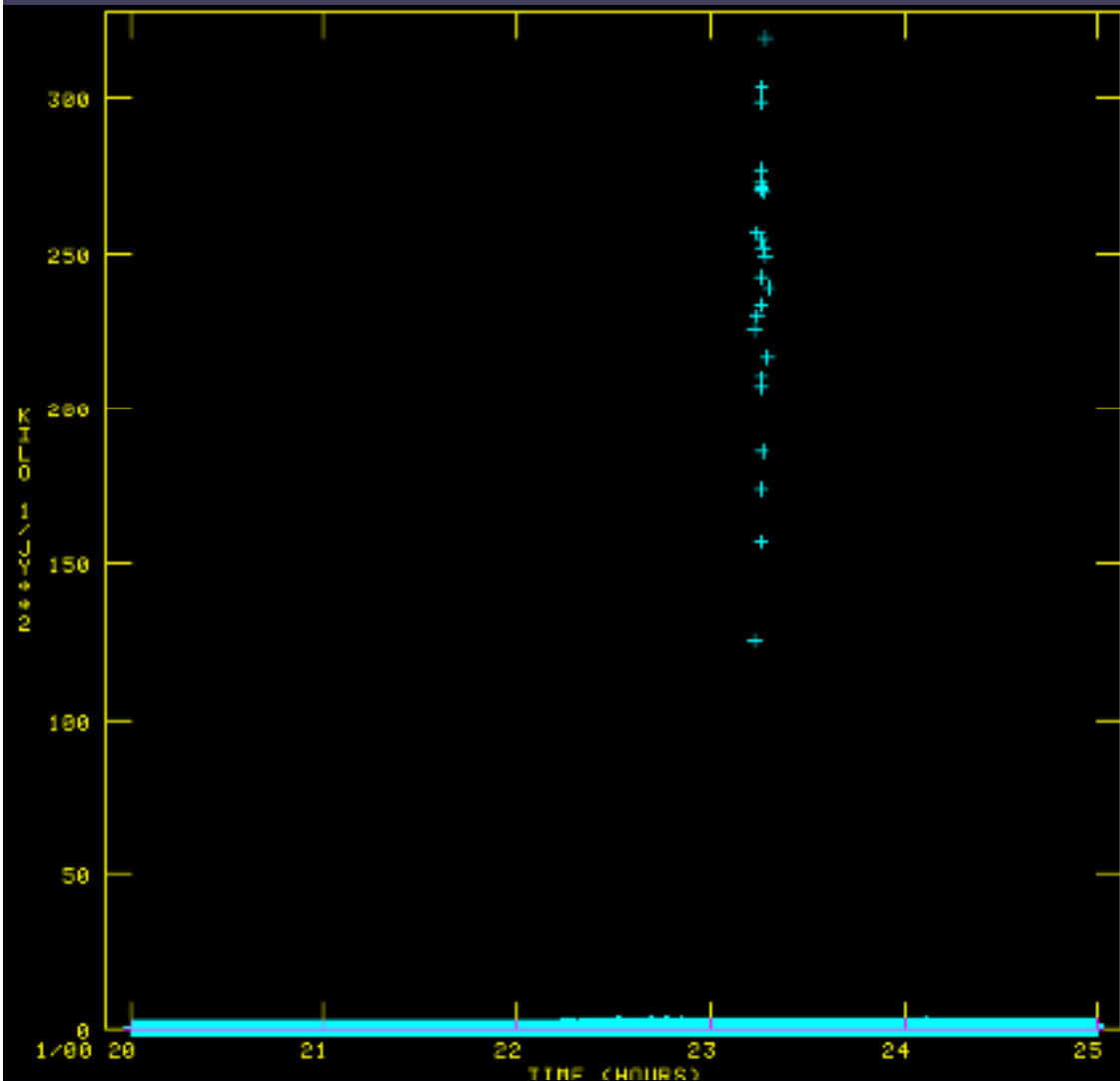


Shows the u-v data from clean image.

Notice that clean does an interpolation in the u-v plane between u-v tracks.

The odd points are smeared, but still present. These produce the low level ripples.

Bad weighting of a few u-v points



After a long search through the data, about 30 points out of 300,000 points were found to have too high of a weight by a factor of 100. Effect is $<1\%$ in image.

Cause??

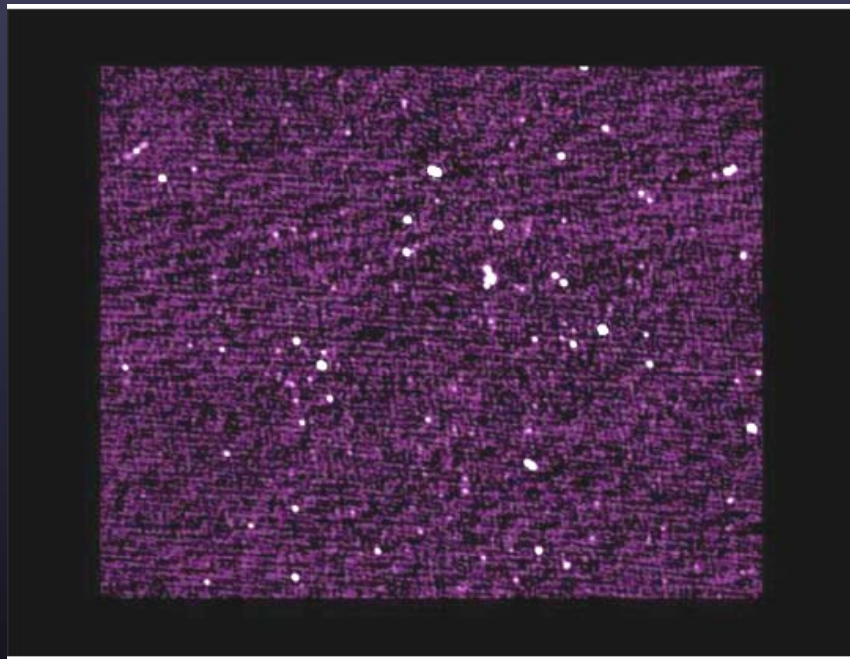
Sometimes in applying calibration produced an incorrect weight in the data. Not present in the original data.

These problems can sneak up on you. Beware.

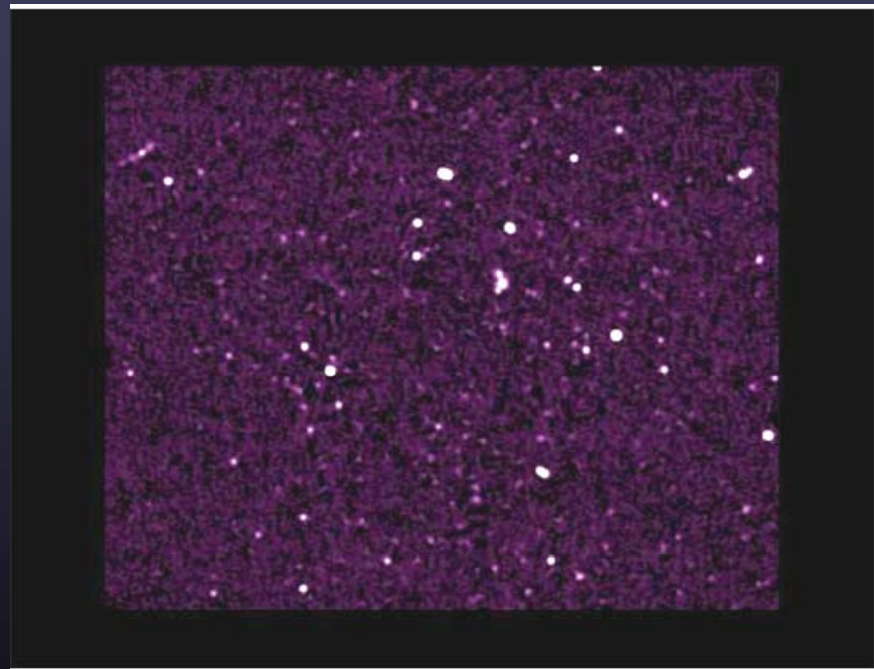
Improvement of Image

Removal of low level ripple improves detectability of faint sources

Before editing



After editing



SUMMARY OF ERROR RECOGNITION

Source structure should be 'reasonable', the rms image noise as expected, and the background featureless. If not,

UV data

Look for outliers in u-v data using several plotting methods.

Check calibration gains and phases for instabilities.

Look at residual data (uv-data - clean components)

IMAGE plane

Do defects resemble the dirty beam?

Are defect properties related to possible data errors?

Are defects related to possible deconvolution problems?

IMAGE ANALYSIS



IMAGE ANALYSIS

- Input: Well-calibrated data-base producing a high quality image
- Output: Parameterization and interpretation of image or a set of images

This is very open-ended

Depends on source emission complexity

Depends on the scientific goals

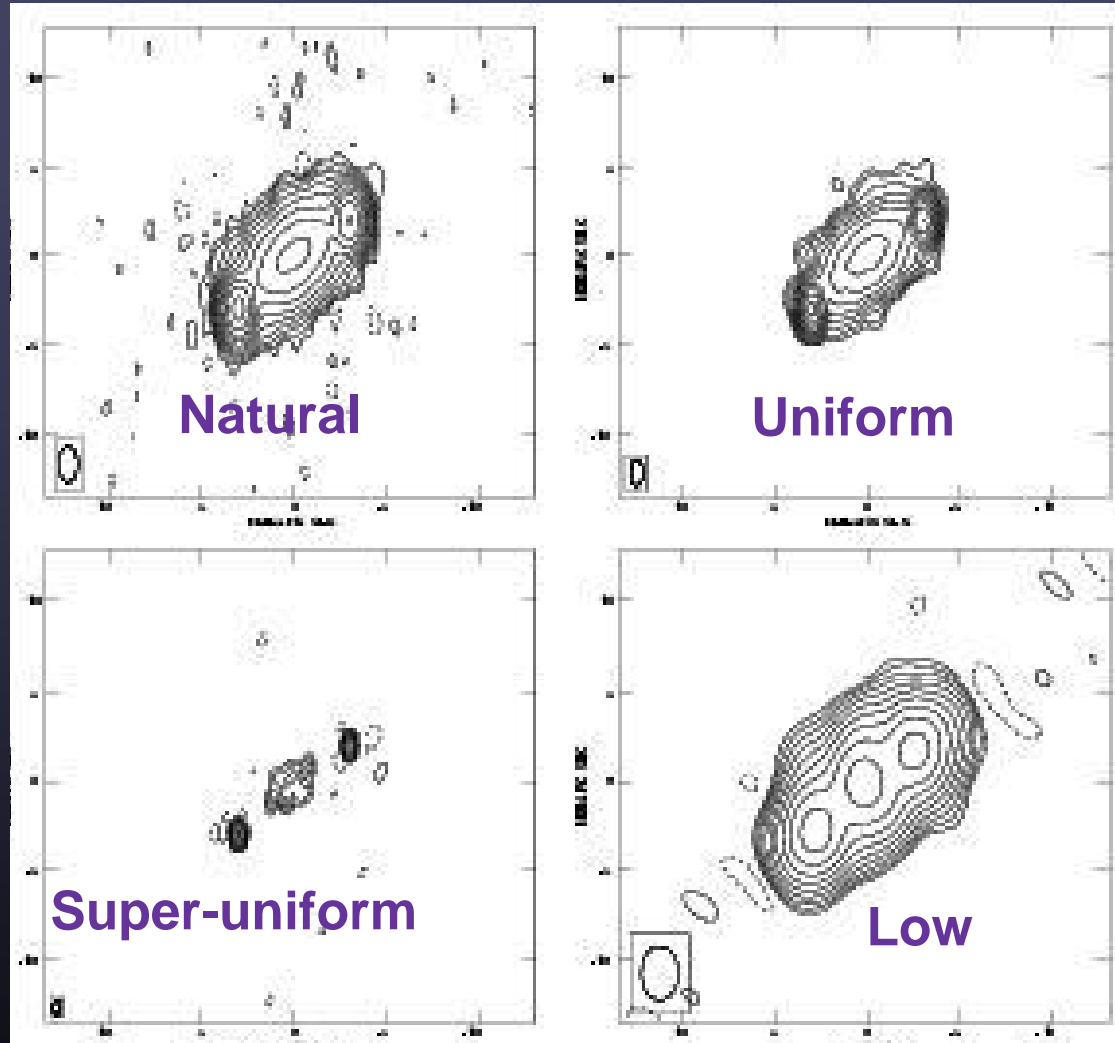
Examples and ideas are given.

Many software packages, besides AIPS and Casa (e.g.. IDL, DS-9) are available.

IMAGE ANALYSIS OUTLINE

- Multi-Resolution of radio source.
- Parameter Estimation of Discrete Components
- Polarization Data
- Image Comparisons
- Positional Registration

IMAGE AT SEVERAL RESOLUTIONS



Milli-arcsec

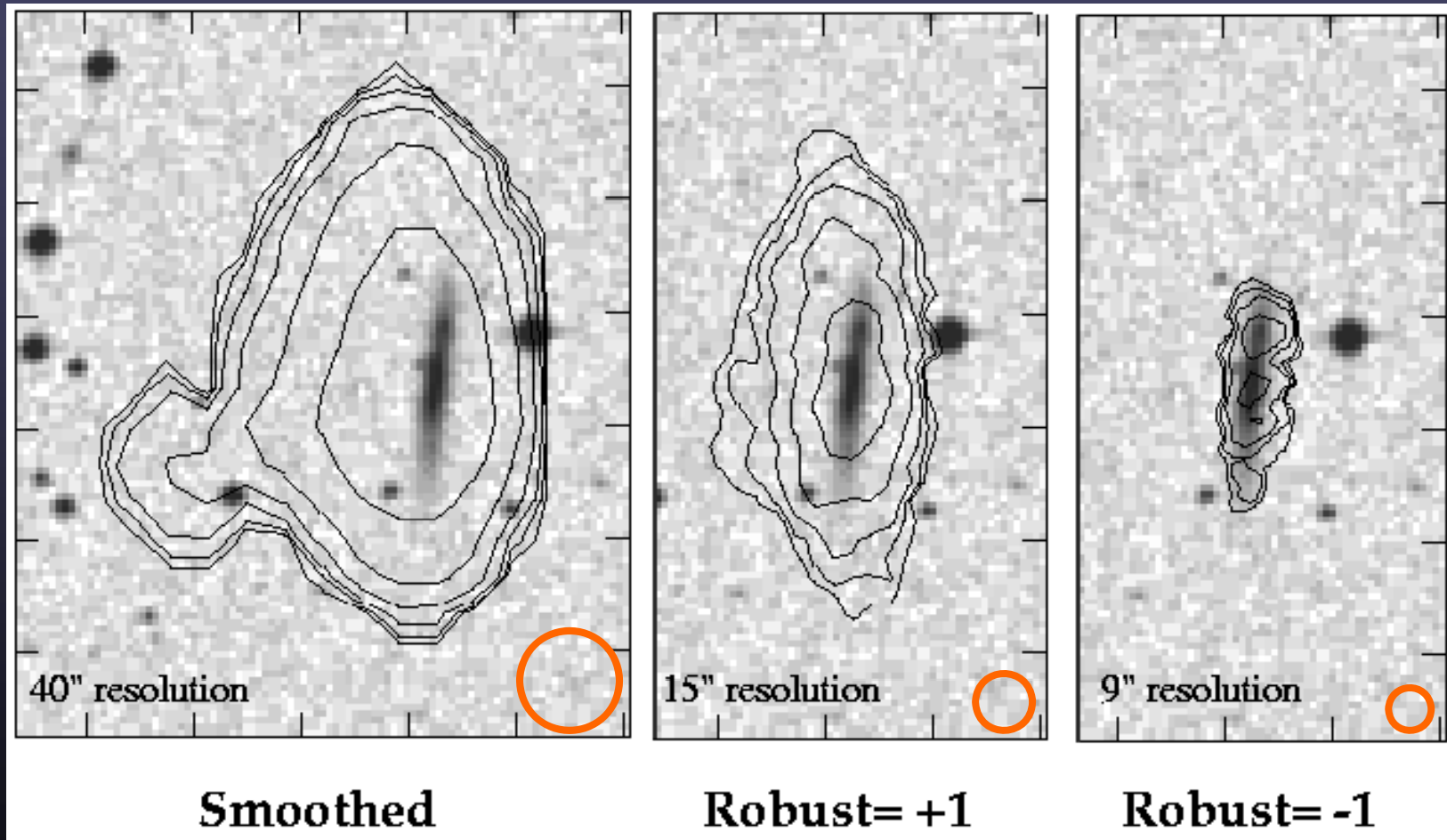
Different aspect of source structure can be seen at various resolutions, shown by the ellipse in the lower left corner of each box.

SAME DATA USED FOR ALL IMAGES

For example,
Outer components are small from SU resolution
There is no extended emission from low resolution

Imaging and Deconvolution of Spectral Line Data:

Type of weighting in imaging



HI contours overlaid on optical images of an edge-on galaxy

PARAMETER ESTIMATION

Parameters associated with discrete components

- **Fitting in the image**
 - Assume source components are Gaussian-shaped
 - Deep cleaning restores image intensity with Gaussian-beam
 - True size * Beam size = Image size, if Gaussian-shaped.
Hence, estimate of true size is relatively simple.
- **Fitting in (u-v) plane**
 - Better estimates for small-diameter sources
 - Can fit to any source model (e.g. ring, disk)
- **Error estimates of parameters**
 - Simple ad-hoc error estimates
 - Estimates from fitting programs

IMAGE FITTING

Component 2-Gaussian

Peak intensity = 0.104 +/- 0.005 JY/BEAM
 Integral intensity= 0.998 +/- 9.47 JANSKYS
 X-position = 255.986 +/- 0.0029 pixels
 Y-position = 257.033 +/- 0.0032 pixels
 Major ax 19.99 +/- 0.02 pixels
 Minor ax 9.98 +/- 0.03 pixels
 Pos ang 135.3 +/- 0.1 deg



Component 1-Gaussian

Peak intensity = 0.300 +/- 0.005 JY/BEAM
 Integral intensity= 0.302 +/- 0.008 JANSKYS
 X-position = 270.991 +/- 0.001 pixels
 Y-position = 267.018 +/- 0.001 pixels
 Major ax 0.53 +/- 0.01 pixels
 Minor ax 0.00 +/- 0.05 pixels
 Pos ang 21.6 +/- 1.1 deg

Component 3-Gaussian

Peak intensity = 0.393 +/- 0.004 JY/BEAM
 Integral intensity= 0.403 +/- 0.008 JANSKYS
 X-position = 241.007 +/- 0.001 pixels
 Y-position = 241.988 +/- 0.001 pixels
 Major ax 1.54 +/- 0.01 pixels
 Minor ax 0.21 +/- 0.01 pixels
 Pos ang 3.6 +/- 0.2 deg

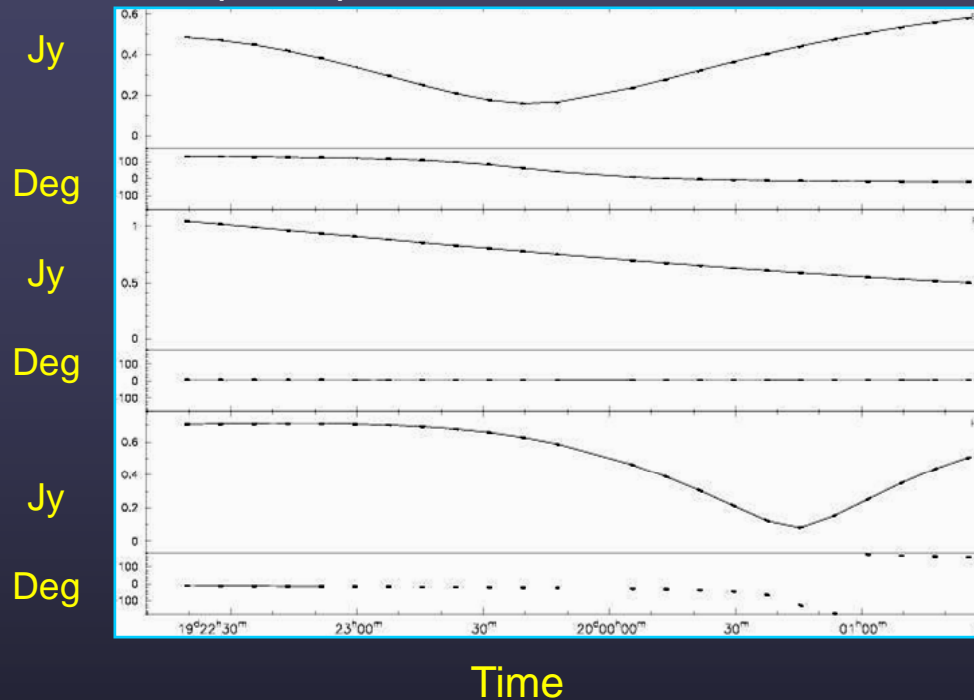
AIPS task: JMFIT

Casa tool

imfit

(U-V) DATA FITTING

Amp and phase vs. time for three baselines



Contour image with model fits



DIFMAP has good u-v fitting algorithm

Fit model directly to (u-v) data

Compare model to data

Contour display of image

Ellipses show true component size. (super-resolution?)

See Greg Taylor's talk at the 12th Synthesis Imaging Workshop, "Non-image Data Analysis"

COMPONENT ERROR ESTIMATES

P = Component Peak Flux Density

σ = Image rms noise

P/σ = signal/noise = S

B = Synthesized beam size

θ_i = Component image size

ΔP = Peak error = σ

ΔX = Position error = $B / 2S$

$\Delta \theta_i$ = Component image size error = $B / 2S$

θ_t = True component size = $(\theta_i^2 - B^2)^{1/2}$

$\Delta \theta_t$ = Minimum component size = $B / S^{1/2}$



Comparison and Combination of Images of Many Types

FORNAX-A Radio/Optical field

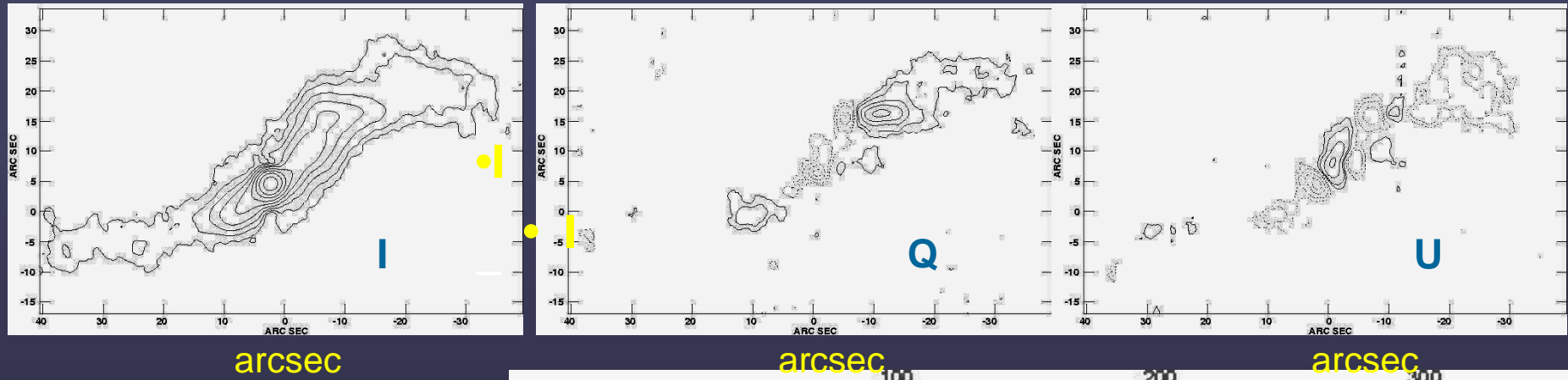
Radio is red
Faint radio core
in center of
NGC1316

Optical in
blue-white

Frame size is
60' x 40'



LINEAR POLARIZATION



Multi-purpose plot

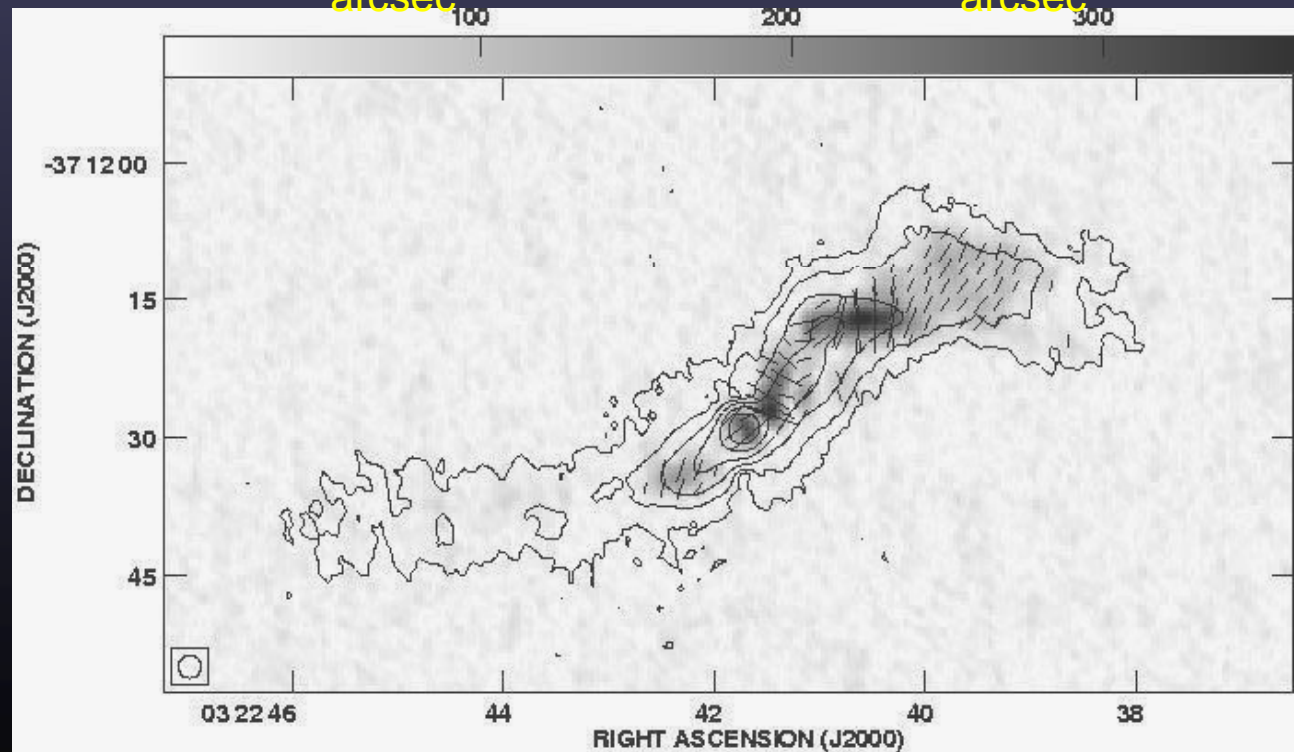
Contours: I,Q,U Pol

Grey scale: P Pol

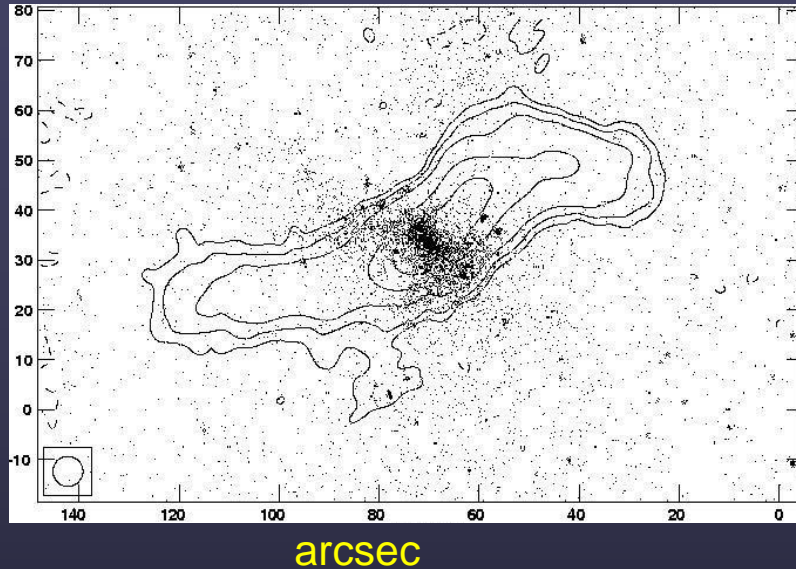
$\sqrt{Q^2+U^2}$ - noise

Line segments – P angle

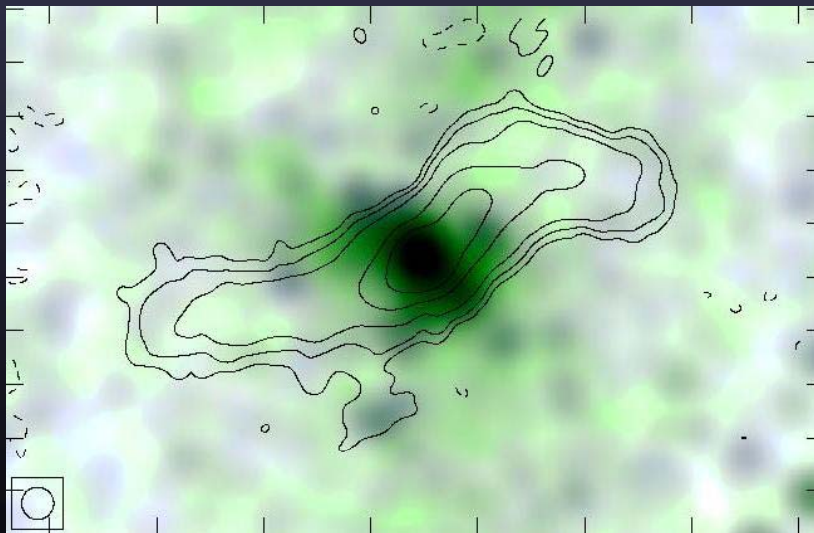
$\text{atan2}(0.5*Q/U)$



COMPARISON OF RADIO/X-RAY IMAGES

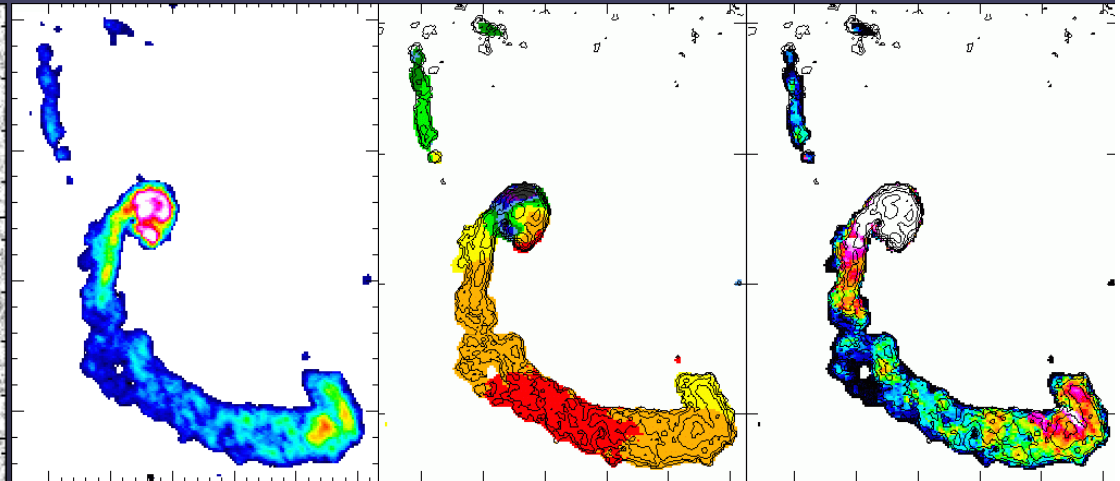
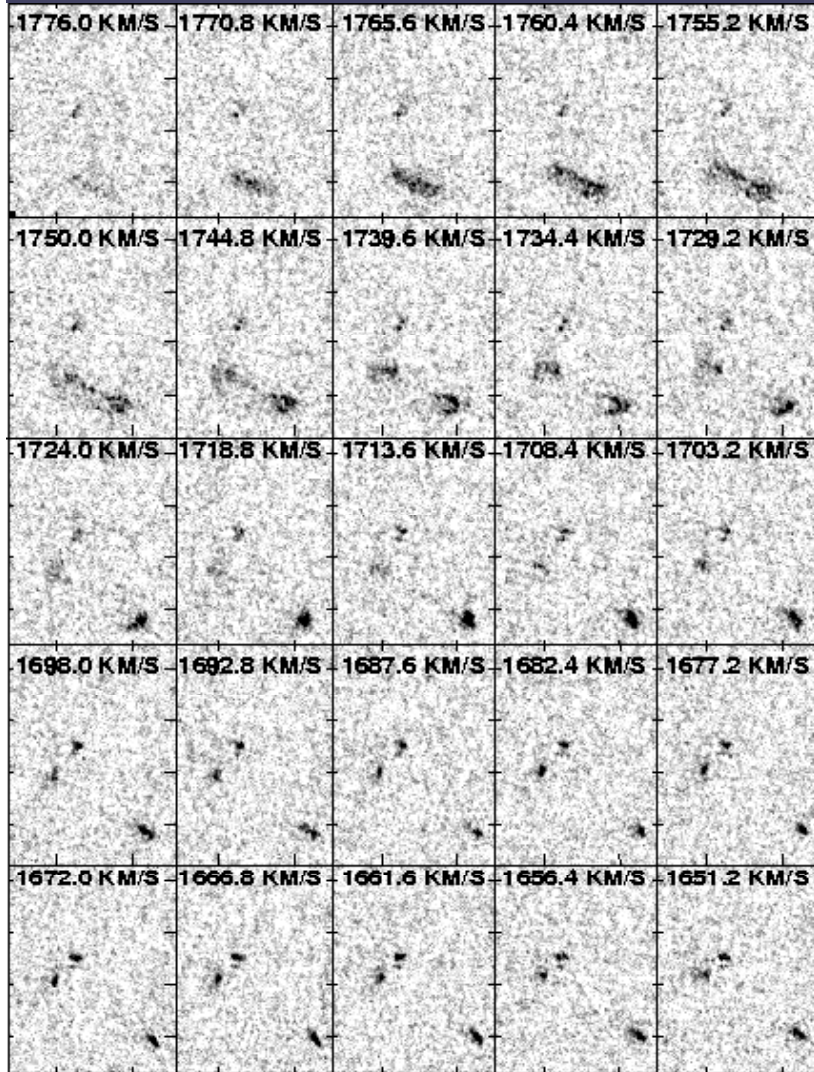


Contours of radio intensity at 5 GHz
Dots represent X-ray Intensity (photons) between 0.7 and 11.0 KeV



Contours of radio intensity at 5 GHz
Color intensity represents X-ray intensity smoothed to radio resolution
Color represents hardness of X-ray (average weighted frequency)
Blue - soft (thermal)
Green - hard (non-thermal)

SPECTRAL LINE REPRESENTATIONS

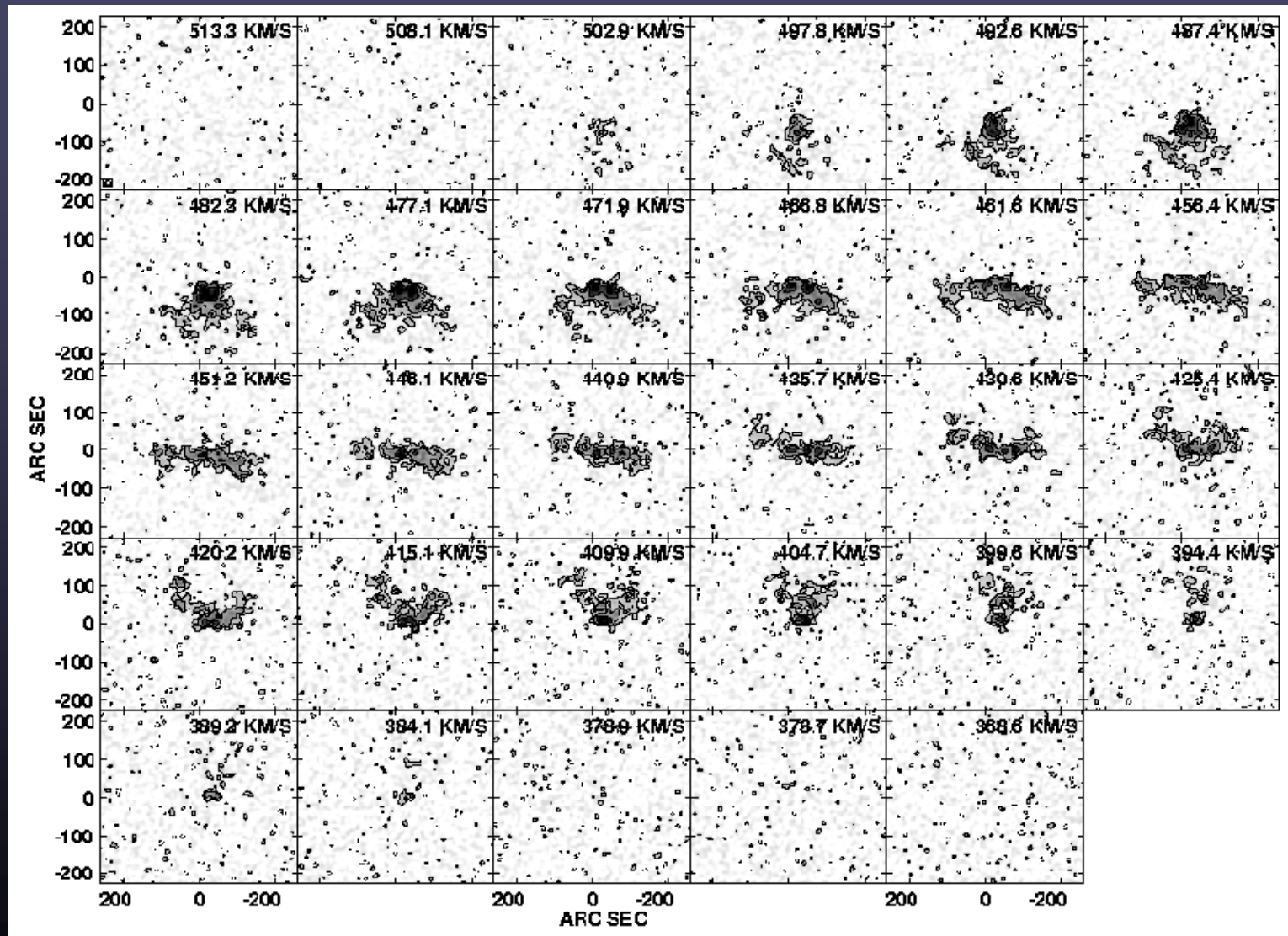


Intensity Image
Sum of velocity
Amount of HI
Red high,
Blue low

Average velocity
Red low vel
Blue high vel
Rotation

Second moment
Velocity width
Turbulence?

Visualizing Spectral Line Data: Channel Images



Greyscale+contour representations of individual channel images

Visualizing Spectral Line Data: Channel Images

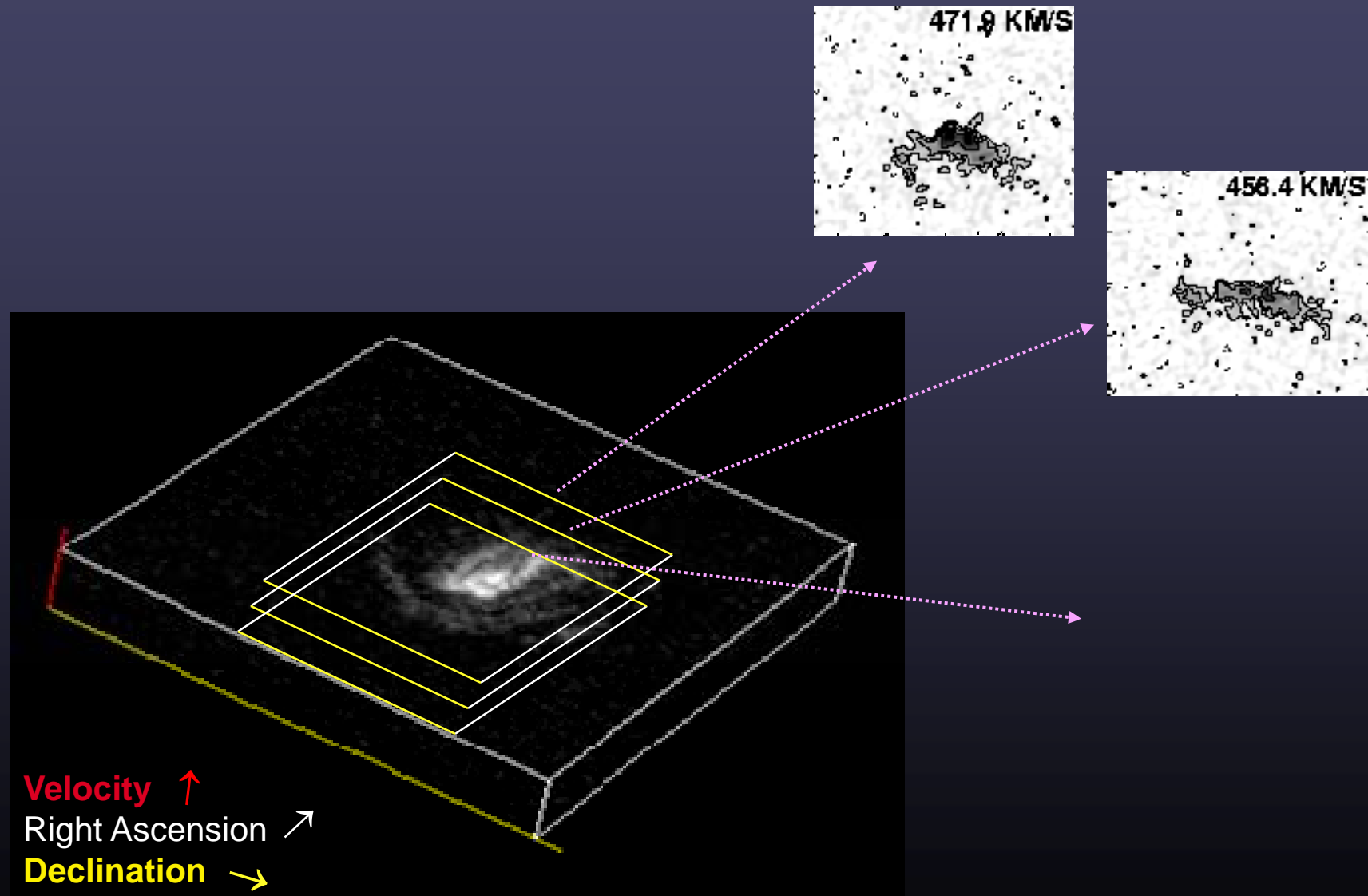


IMAGE REGISTRATION AND ACCURACY

- **Separation Accuracy of Components on One Image due to residual phase errors, regardless of signal/noise:**

Limited to 1% of resolution

Position errors of 1:10000 for wide fields, i.e. 0.1" over 1.4 GHz PB

- **Images at Different Frequencies:**

Multi-frequency. Use same calibrator for all frequencies.

Watch out at frequencies < 2 GHz when ionosphere can produce displacement. Minimize calibrator-target separation

- **Images at Different Times (different configuration):**

Use same calibrator for all observations. Daily troposphere changes can produce position changes up to 25% of the resolution.

- **Radio versus non-Radio Images:**

Header-information of non-radio images often much less accurate than that for radio. For accuracy $< 1''$, often have to align using coincident objects.

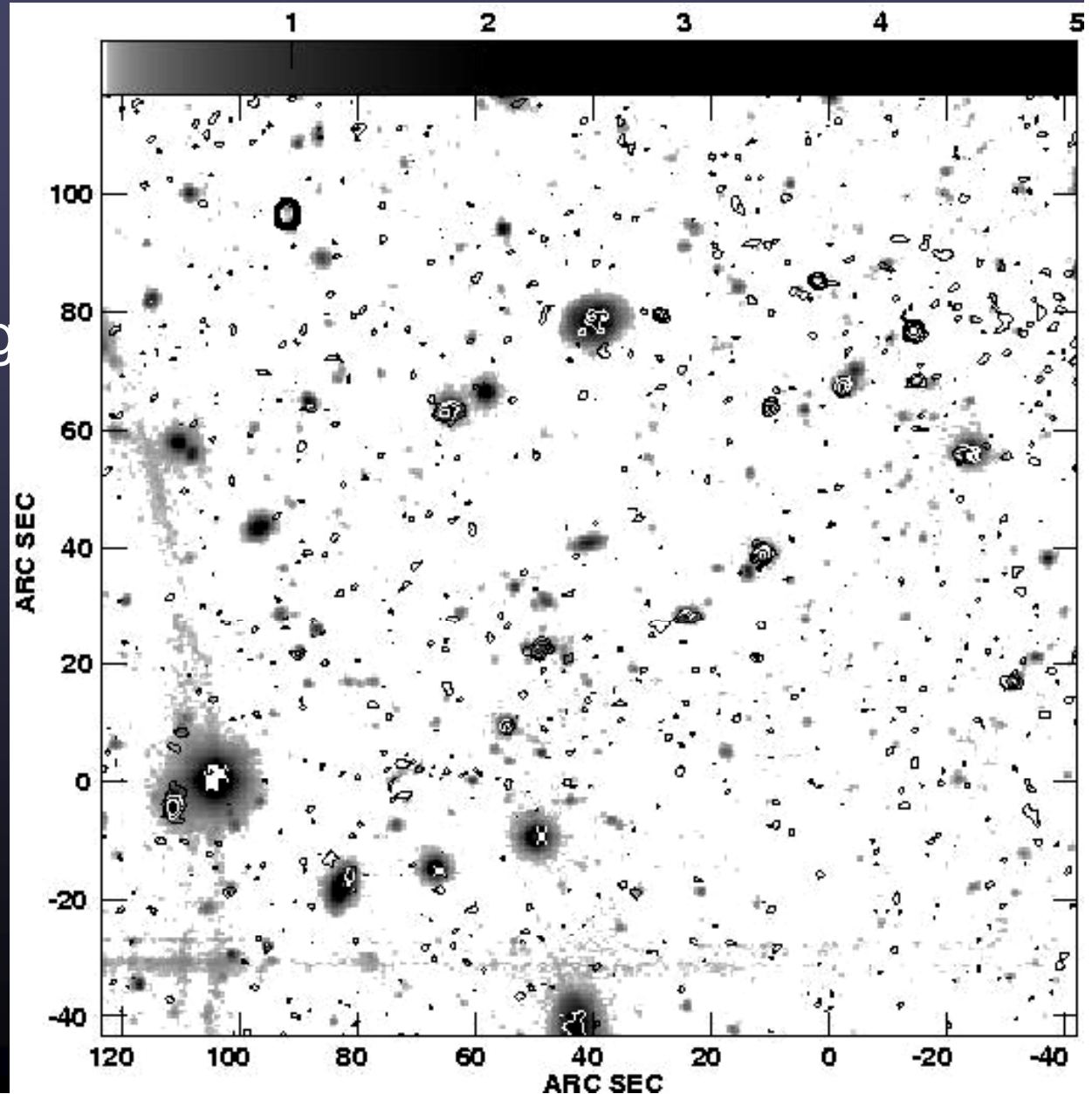
DEEP RADIO / OPTICAL COMPARISON

Grey-Scale:

Optical emission
faintest is 26-mag

Contours:

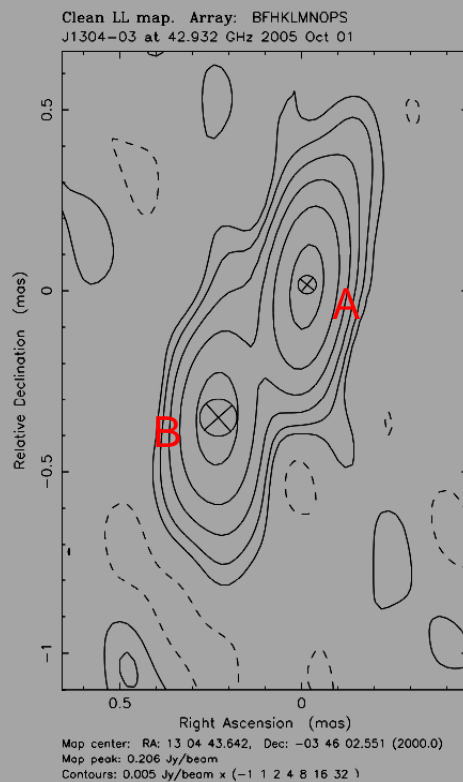
Radio Emission
faintest is $10 \mu\text{Jy}$



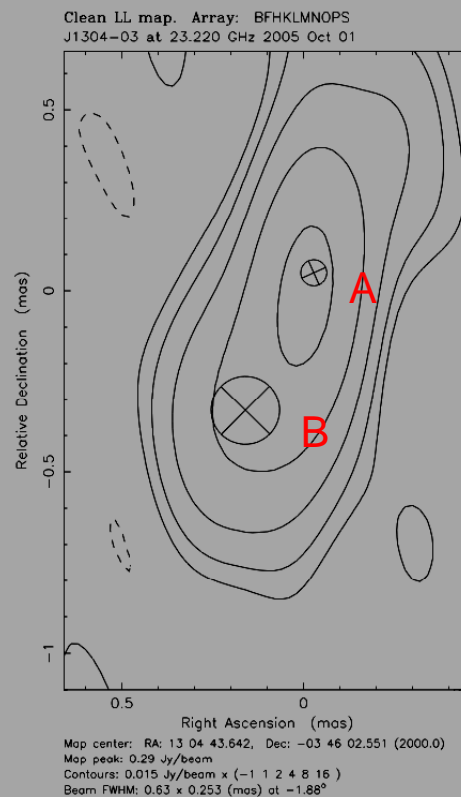
Radio Source Alignment at Different Frequencies

Self-calibration at each frequency aligns maximum at (0,0) point
Frequency-dependent structure causes relative position of maximum to change
Fitting of image with components can often lead to proper registration

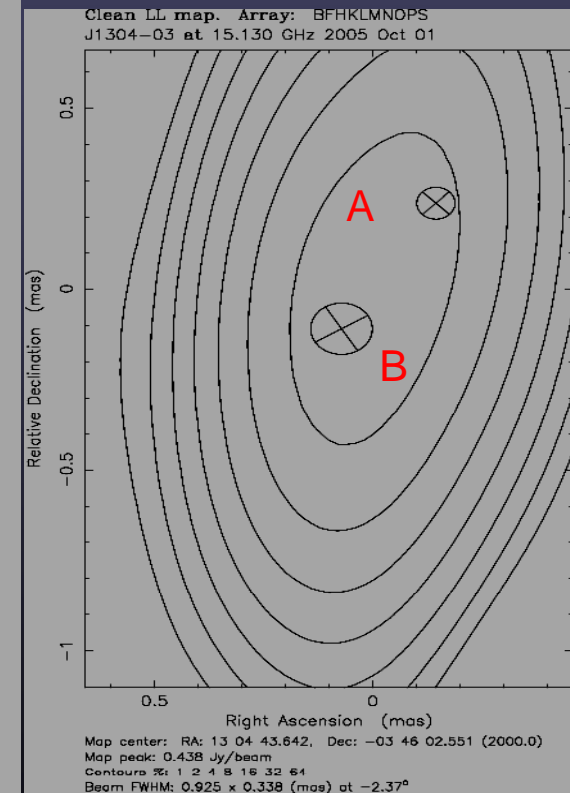
43 GHz: res = 0.3 mas



23 GHz: res = 0.6 mas



15 GHz: res = 0.8 mas



SUMMARY

- Analyze and display data in several ways
Adjust resolution to illuminate desired interpretation, analysis
- Parameter fitting useful, but try to obtain error estimate
Fitting in u-v plane, image plane
- Comparison of multi-plane images tricky (Polarization and Spectral Line)
Use different graphics packages, methods, analysis tools
- Registration of a field at different frequencies or wave-bands can be subtle.
Often use ad hoc methods by aligning 'known' counterparts